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# Lösungen

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**1**

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**a**

$$\begin{aligned} D[a5 t^{5+3} t^4 + 2 x^{2+a2} t^{2-8 t-11}, t] \\ -8 + 2 a2 t + 12 t^3 + 5 a5 t^4 \end{aligned}$$

**b**

$$\begin{aligned} D[\tan[x] - e^x + e^{-x} - 1/2, x] \\ -e^{-x} - e^x + \sec^2[x] \end{aligned}$$

**v**

$$\begin{aligned} D[\cos[x] - \log[\pi x] \sqrt{x}, x] \\ -\frac{1}{\sqrt{x}} - \frac{\log[\pi x]}{2\sqrt{x}} - \sin[x] \end{aligned}$$

**d**

$$\begin{aligned} D[\sin[x] \log[x] - e^x/x, x] \\ \frac{e^x}{x^2} - \frac{e^x}{x} + \cos[x] \log[x] + \frac{\sin[x]}{x} \end{aligned}$$

**e**

$$\begin{aligned} D[\sin[3 e^x] + 2 e^{-x^3} x^2, x] \\ -6 e^{-x^3} x^2 + 3 e^x \cos[3 e^x] \end{aligned}$$

**f**

$$D[\arcsin[-\sin[x]], x]$$

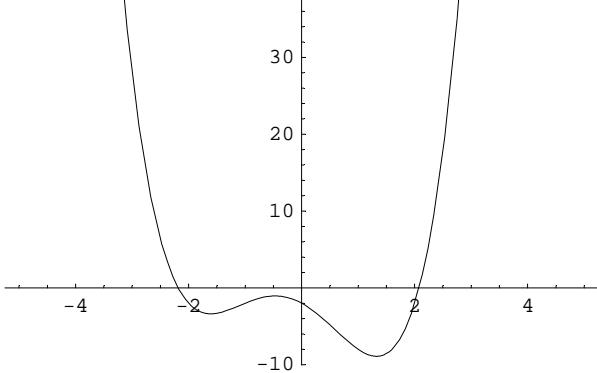
$$-\frac{\cos[x]}{\sqrt{1 - \sin^2[x]}}$$

```
D[ArcSin[-Sin[x]],x]/.x->1.0
```

```
-1.
```

## 2

```
f[x]:= (x-2) x (x+1) (x+2)-2
Plot[(x-2) x (x+1) (x+2)-2,{x,-5,5}];
```



```
FindRoot[f[x]==0,{x,-2}]
```

```
{x → -2.18467}
```

```
FindRoot[f[x]==0,{x,2}]
```

```
{x → 2.07678}
```

```
Solve[(x-2) x (x+1) (x+2)==0,{x}]
```

```
{ {x → -2}, {x → -1}, {x → 0}, {x → 2} }
```

```
(x-2) x (x+1) (x+2)//Expand
```

```
-4 x - 4 x2 + x3 + x4
```

```
D[(x-2) x (x+1) (x+2),x]
```

```
(-2 + x) x (1 + x) + (-2 + x) x (2 + x) + (-2 + x) (1 + x) (2 + x) + x (1 + x) (2 + x)
```

```
D[(x-2) x (x+1) (x+2),x]//Expand
```

```
-4 - 8 x + 3 x2 + 4 x3
```

```
Solve[Evaluate[D[(x-2) x (x+1) (x+2)-2,x]==0],{x}]
```

$$\left\{ x \rightarrow -\frac{1}{4} + \frac{7 \sqrt[3]{5}}{4 \left( 3 \left( 27 + 8 \sqrt[3]{69} \right) \right)^{1/3}} + \frac{\left( 5 \left( 27 + 8 \sqrt[3]{69} \right) \right)^{1/3}}{4 \sqrt[3]{3^2}}, \right.$$

$$\left. x \rightarrow -\frac{1}{4} - \frac{7 \sqrt[3]{5} \left( 1 + \sqrt[3]{3} \right)}{8 \left( 3 \left( 27 + 8 \sqrt[3]{69} \right) \right)^{1/3}} - \frac{\left( 1 - \sqrt[3]{3} \right) \left( 5 \left( 27 + 8 \sqrt[3]{69} \right) \right)^{1/3}}{8 \sqrt[3]{3^2}} \right\},$$

$$\left. x \rightarrow -\frac{1}{4} - \frac{7 \sqrt[3]{5} \left( 1 - \sqrt[3]{3} \right)}{8 \left( 3 \left( 27 + 8 \sqrt[3]{69} \right) \right)^{1/3}} - \frac{\left( 1 + \sqrt[3]{3} \right) \left( 5 \left( 27 + 8 \sqrt[3]{69} \right) \right)^{1/3}}{8 \sqrt[3]{3^2}} \right\}$$

```

solv1=Solve[Evaluate[D[(x-2) x (x+1) (x+2)-2,x]==0],{x}]/.N//Chop//Flatten
{x → 1.32635, x → -1.60725, x → -0.469093}

Table[f[x]/.solv1[[k]],{k,1,3}]
{-8.9141, -3.38275, -1.05862}

D[(x-2) x (x+1) (x+2),{x,2}]
2 (-2 + x) x + 2 (1 + x) (2 + x) + 2 (-2 + 2 x) (3 + 2 x)

D[(x-2) x (x+1) (x+2),{x,2}]/.Expand
-8 + 6 x + 12 x2

solv2=Solve[Evaluate[D[(x-2) x (x+1) (x+2),{x,2}]==0],{x}]/.N//Chop//Flatten
{x → -1.10391, x → 0.603913}

Table[f[x]/.solv2[[k]],{k,1,2}]
{-2.31905, -5.52122}

```

**3**

```

f[x_]:=x^5

Plot[x^5,{x,-1.5,1.5}];



```

```

t[x_,x0_]:=Evaluate[f'[x0](x-x0)+f[x0]]

t[x,x0]
5 (x - x0) x04 + x05

Solve[t[x,x0]==0,{x}]
{ {x →  $\frac{4 x_0}{5}$  } }

t[0,x0]
-4 x05

n[x_,x0_]:=Evaluate[-1/f'[x0](x-x0)+f[x0]]

```

---

```
solv=Solve[n[x,x0]==0,{x}]//Flatten
{x → x0 (1 + 5 x08) }
```

n[0,x0]

$$\frac{1}{5 x0^3} + x0^5$$

**1**

(x0-4/5 x0)f[x0]/2

$$\frac{x0^6}{10}$$

(x0-4/5 x0)f[x0]/2 /.x0->2.

6.4

**2**

4/5 x0 (-4x0<sup>5</sup>)/2

$$-\frac{8 x0^6}{5}$$

4/5 x0 (-4x0<sup>5</sup>)/2 /.x0->2.

-102.4

**3**

n[0,x0] x/2/.solv

$$\frac{1}{2} x0 \left( \frac{1}{5 x0^3} + x0^5 \right) (1 + 5 x0^8)$$

n[0,x0] x/2/.solv /.x0->2.

41024.

n[0,x0] x/2/.solv //Expand

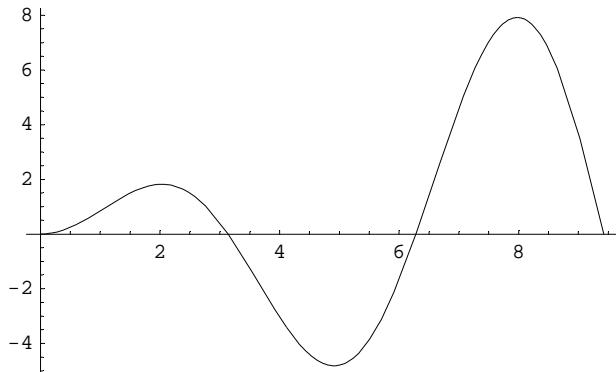
$$\frac{1}{10 x0^2} + x0^6 + \frac{5 x0^{14}}{2}$$

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**4**

f[x\_]:=x Sin[x]

```
Plot[f[x],{x,0,3Pi}];
```



```
D[x Sin[x],x]
```

$$x \cos(x) + \sin(x)$$

```
fr=FindRoot[Evaluate[D[x Sin[x],x]==0],{x,0}]
```

$$\{x \rightarrow 0.\}$$

```
f[x]/.fr
```

$$0.$$

```
fr=FindRoot[Evaluate[D[x Sin[x],x]==0],{x,2}]
```

$$\{x \rightarrow 2.02876\}$$

```
f[x]/.fr
```

$$1.81971$$

```
fr=FindRoot[Evaluate[D[x Sin[x],x]==0],{x,5}]
```

$$\{x \rightarrow 4.91318\}$$

```
f[x]/.fr
```

$$-4.81447$$

```
fr=FindRoot[Evaluate[D[x Sin[x],x]==0],{x,8}]
```

$$\{x \rightarrow 7.97867\}$$

```
f[x]/.fr
```

$$7.91673$$

```
D[x Sin[x],{x,2}]
```

$$2 \cos(x) - x \sin(x)$$

```
fr=FindRoot[Evaluate[D[x Sin[x],{x,2}]==0],{x,1}]
```

$$\{x \rightarrow 1.07687\}$$

```
f[x]/.fr
```

$$0.948166$$

```
fr=FindRoot[Evaluate[D[x Sin[x],{x,2}]==0],{x,4}]
{x → 3.6436}

f[x]/.fr
-1.75324

fr=FindRoot[Evaluate[D[x Sin[x],{x,2}]==0],{x,6}]
{x → 6.57833}

f[x]/.fr
1.91352

fr=FindRoot[Evaluate[D[x Sin[x],{x,2}]==0],{x,9}]
{x → 9.62956}

f[x]/.fr
-1.95821
```

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## 5

```
Limit[(4x+Tan[2x])/Sin[x],x->0]
6

Limit[α (x^3+x^2-2+Log[x-1])/(Pi x^3-Pi),x->1]
α (-∞)
```