

# Lösungen

In[70]:= Remove["Global`\*"]

## 1

In[71]:= DSolve[y'[x] == x y[x]^3, y[x], x]

$$\text{Out}[71]= \left\{ \left\{ Y[x] \rightarrow -\frac{1}{\sqrt{-x^2 - 2 C[1]}} \right\}, \left\{ Y[x] \rightarrow \frac{1}{\sqrt{-x^2 - 2 C[1]}} \right\} \right\}$$

In[72]:= DSolve[{y'[x] == x y[x]^3, y[1] == 1}, y[x], x]

$$\text{Out}[72]= \left\{ \left\{ Y[x] \rightarrow \frac{1}{\sqrt{2 - x^2}} \right\} \right\}$$

In[73]:= DSolve[{y'[x]==x y[x]^3,y[1]==1},y,x]

$$\text{Out}[73]= \left\{ \left\{ Y \rightarrow \text{Function}\left[\{x\}, \frac{1}{\sqrt{2 - x^2}}\right] \right\} \right\}$$

In[74]:= u[x\_, c\_] := Re[PowerExpand[(c / x)^(1/3)]]; u[x, c]

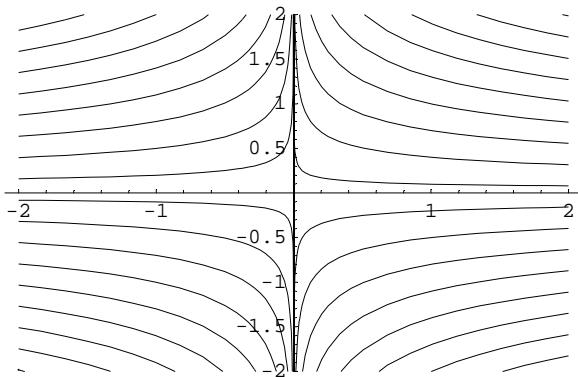
$$\text{Out}[74]= \text{Re}\left[\frac{C^{1/3}}{x^{1/3}}\right]$$

In[75]:= u[x\_, c\_] := Abs[(c / x)]^(1/3) Sign[x c]; u[x, c]

$$\text{Out}[75]= \text{Abs}\left[\frac{C}{x}\right]^{1/3} \text{Sign}[c x]$$

In[76]:= g1 =

Plot[Evaluate[Table[u[x, c^3], {c, -5, 5, 0.3}]], {x, -2, 2}, PlotRange -> {-2, 2}];



In[77]:= h[x\_]:=ToRadicals[Table[Root[1/x^3 - c, 1],{c,1,5}]];

In[78]:= 1/ToRadicals[Table[Root[x^3 - c, 1],{c,1,5}]//N

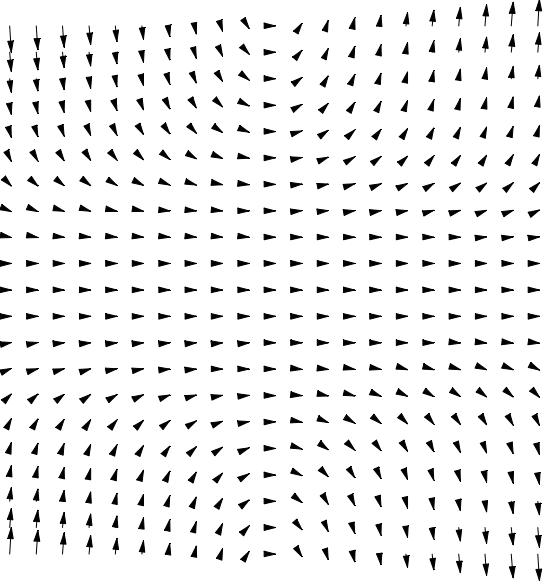
$$\text{Out}[78]= \{1., 0.793701, 0.693361, 0.629961, 0.584804\}$$

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In[79]:= ToRadicals[Table[Root[x^3 - c, 1], {c, 1, 5}]]//N
Out[79]= {1., 1.25992, 1.44225, 1.5874, 1.70998}

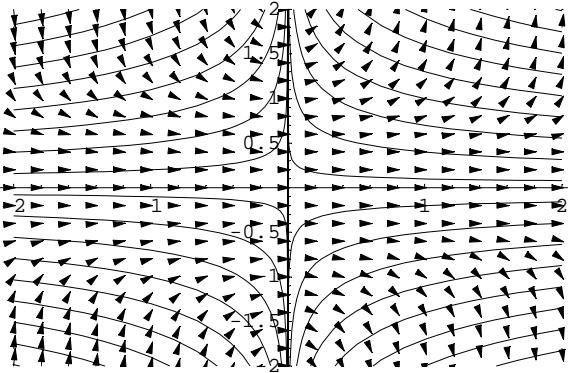
In[80]:= ?Root
Root[f, k] represents the kth root of the polynomial equation f[x] == 0. Mehr...
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In[81]:= << Graphics`PlotField`
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In[82]:= g2=PlotVectorField[{1, x y^3},{x,-2,2,0.2},{y,-2,2,0.2}];
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In[83]:= Show[g1, g2];
```



## 2

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In[84]:= DSolve[{y'[x]==Cos[x]/y[x]},y,x]
Out[84]= {{y->Function[{x}, -Sqrt[2] Sqrt[C[1] + Sin[x]]]}, {y->Function[{x}, Sqrt[2] Sqrt[C[1] + Sin[x]]]}}
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In[85]:= DSolve[{y'[x]==Cos[x]/y[x],y[0]==4},y[x],x]
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Out[85]= {{y[x] -> Sqrt[2] Sqrt[8 + Sin[x]]}}
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In[86]:= DSolve[{y'[x] == Cos[x]/y[x], y[0] == 4}, y, x]
Out[86]= {y → Function[{x}, Sqrt[2] Sqrt[8 + Sin[x]]]}
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**3****a**

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In[87]:= DSolve[{y[x] + 4x + y'[x] x == 0}, y[x], x] // Simplify
Out[87]= {y[x] → -2x + C[1]/x}
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**b**

$$y = -2x$$


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**4**

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In[88]:= Remove["Global`*"]
In[89]:= DSolve[{y''[x] - y'[x] + y[x] == E^(-x)}, y[x], x] // Simplify
Out[89]= {y[x] → (E^-x + E^(x/2) C[1] Cos[x/2] + E^(x/2) C[2] Sin[x/2])}
In[90]:= DSolve[{y''[x] - y'[x] + y[x] == E^(-x), y[0] == 0, y'[0] == 0}, y[x], x] // Simplify
Out[90]= {y[x] → (1/3 (E^-x - E^(x/2) Cos[x/2] + Sqrt[3] E^(x/2) Sin[x/2]))}
In[91]:= solv=DSolve[{y''[x]-y'[x]+y[x]==E^(-x),y[0]==0,y'[0]==0},y,x]//Simplify//Flatten
Out[91]= {y → Function[{x},
-1/3 E^-x (E^(3x/2) Cos[x/2] - Cos[x/2]^2 - Sqrt[3] E^(3x/2) Sin[x/2] - Sin[x/2]^2)]}
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Wichtig: Am Schluss steht ....y,x ]//Simplify//Flatten und nicht ....y[x],x ]//Simplify//Flatten

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In[92]:= y=y/.solv;
y[z]
Out[93]= -1/3 E^-z (E^(3z/2) Cos[z/2] - Cos[z/2]^2 - Sqrt[3] E^(3z/2) Sin[z/2] - Sin[z/2]^2)
In[94]:= y[1]
Out[94]= -1/(3 E^(3/2)) (E^(3/2) Cos[z/2] - Cos[z/2]^2 - Sqrt[3] E^(3/2) Sin[z/2] - Sin[z/2]^2)
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In[95]:= y[1]/N
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Out[95]= 0.491691
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In[96]:= pl=Plot[y[z],{z,0,10}];
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