

# MP06 Bau1 - Lösungen / ähnliche Lösungen / Lösungen von ev. weiteren Aufgaben

---

## 1 Differenzieren und integrieren

### a Resultat so kurz wie möglich halten

```
f[x_]:=x^2+ 0.5 Sin[x];  
f[x]
```

$$x^2 + 0.5 \sin[x]$$

```
f'[x]
```

$$2x + 0.5 \cos[x]$$

```
f'[x]/.x->1
```

$$2.27015$$

```
ArcTan[f'[x]/.x->1]
```

$$1.15587$$

```
ArcTan[f'[x]/.x->1]/Degree
```

$$66.2265$$

```
f''[x]/.x->1
```

$$1.57926$$

### b Resultat so kurz wie möglich halten

```
f[x_]:=(((x^(3/4)-3)^3)^(1/4))^5
```

```
f[x]
```

$$\left((-3 + x^{3/4})^3\right)^{5/4}$$

```
D[f[x],x]//Simplify
```

$$\frac{45 (-3 + x^{3/4})^2 \left(-3 + x^{3/4}\right)^{1/4}}{16 x^{1/4}}$$

**D[f[x],x]//Expand**

$$\frac{405 \left( (-3 + x^{3/4})^3 \right)^{1/4}}{16 x^{1/4}} - \frac{135}{8} \left( (-3 + x^{3/4})^3 \right)^{1/4} \sqrt{x} + \frac{45}{16} \left( (-3 + x^{3/4})^3 \right)^{1/4} x^{5/4}$$

### c Resultat so kurz wie möglich halten

**f[x\_] := 4 x^2 Sin[3x^2-2]**

**f[x]**

$$-4 x^2 \text{Sin}[2 - 3 x^2]$$

**D[f[x],x]//Simplify**

$$24 x^3 \text{Cos}[2 - 3 x^2] - 8 x \text{Sin}[2 - 3 x^2]$$

**D[f[x],x]//Expand**

$$24 x^3 \text{Cos}[2 - 3 x^2] - 8 x \text{Sin}[2 - 3 x^2]$$

### d Resultat so kurz wie möglich halten

**f[x\_] := Log[x/(1-x)] (x/(1-x))**

**f[x]**

$$\frac{x \text{Log}\left[\frac{x}{1-x}\right]}{1-x}$$

**D[f[x],x]//Simplify**

$$\frac{1 + \text{Log}\left[\frac{x}{1-x}\right]}{(-1+x)^2}$$

**D[f[x],x]//Expand**

$$\frac{1}{1-x} + \frac{x}{(1-x)^2} + \frac{\text{Log}\left[\frac{x}{1-x}\right]}{1-x} + \frac{x \text{Log}\left[\frac{x}{1-x}\right]}{(1-x)^2}$$

### e Resultat so kurz wie möglich halten

**f[x\_] := 4 E^(-x) Cos[2-E^x]**

**f[x]**

$$4 e^{-x} \text{Cos}[2 - e^x]$$

**D[f[x],x]//Simplify**

$$-4 e^{-x} \text{Cos}[2 - e^x] + 4 \text{Sin}[2 - e^x]$$

**D[f[x],x]//Expand**

$$-4 e^{-x} \text{Cos}[2 - e^x] + 4 \text{Sin}[2 - e^x]$$

## f Resultat so kurz wie möglich halten

```
Remove[a]

f[x_]:= x^2+a Sin[x]+2/x

Integrate[f[x],{x,1,E^2}]


$$\frac{1}{3} (11 + e^6 + 3 a \text{Cos}[1] - 3 a \text{Cos}[e^2])$$


Integrate[f[x],{x,1,E^2}]/Expand


$$\frac{11}{3} + \frac{e^6}{3} + a \text{Cos}[1] - a \text{Cos}[e^2]$$

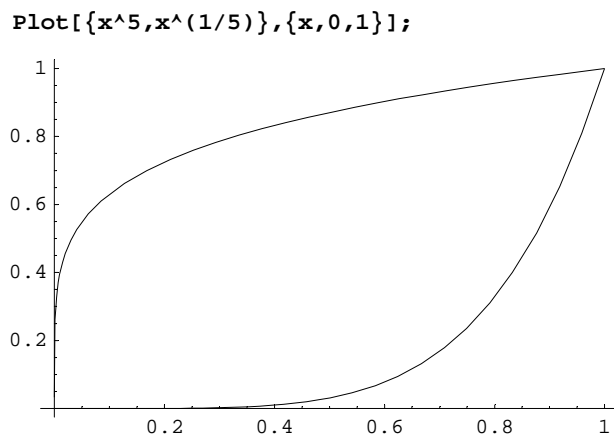

N[%]/Expand

138.143 + 0.0919461 a
```

## 2 Kurven und Flächen

Gegeben sei die Kurvenschar  $y=x^a$  auf  $I=[0,1]$

### a Plot



### b $y=x^a$ soll die eingeschlossene Fläche halbieren. Berechne a

```
r1=Evaluate[Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[1]][[2]]];
r2=Evaluate[Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[2]][[2]]];
h=(r1==r2)
```

$$\frac{1}{6} - \frac{1}{1+a} = -\frac{5}{6} + \frac{1}{1+a}$$

Solve[h,{a}]

{a → 1}

r1=Evaluate[Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[1]][[2]]];

r2=Evaluate[

Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[2]][[2]]];

h=(r1==3 r2)

$$\frac{1}{6} - \frac{1}{1+a} = 3 \left( -\frac{5}{6} + \frac{1}{1+a} \right)$$

Solve[h,{a}]

{a →  $\frac{1}{2}$ }

r1=Evaluate[Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[1]][[2]]];

r2=Evaluate[

Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[2]][[2]]];

h=(r1==(Sqrt[5]+1)/2 r2)

$$\frac{1}{6} - \frac{1}{1+a} = \frac{1}{2} (1 + \sqrt{5}) \left( -\frac{5}{6} + \frac{1}{1+a} \right)$$

solv1=Solve[h,{a}]/Flatten

{a →  $\frac{11 + \sqrt{5}}{7 + 5\sqrt{5}}$ }

N[%]

{a → 0.728043}

r3=Evaluate[Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[1]][[2]]];

r4=Evaluate[

Integrate[x^5-x^(a),{x,0,1}]==Integrate[x^(a)-x^(1/5),{x,0,1}]][[2]][[2]]];

h=(r3==(Sqrt[5]-1)/2 r2)

$$\frac{1}{6} - \frac{1}{1+a} = \frac{1}{2} (-1 + \sqrt{5}) \left( -\frac{5}{6} + \frac{1}{1+a} \right)$$

N[%]

$$0.166667 - \frac{1}{1+a} = 0.618034 \left( -0.833333 + \frac{1}{1+a} \right)$$

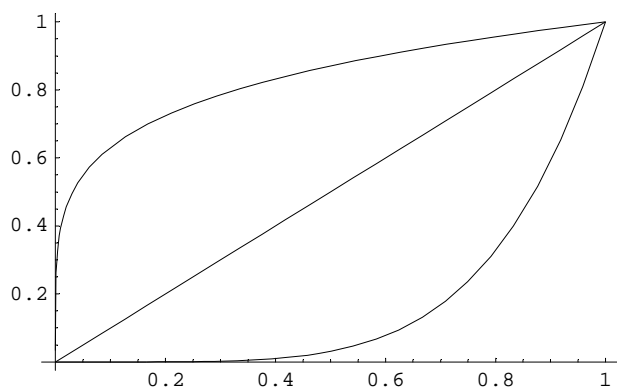
solv2=Solve[h,{a}]/Flatten

{a →  $\frac{9 + \sqrt{5}}{-3 + 5\sqrt{5}}$ }

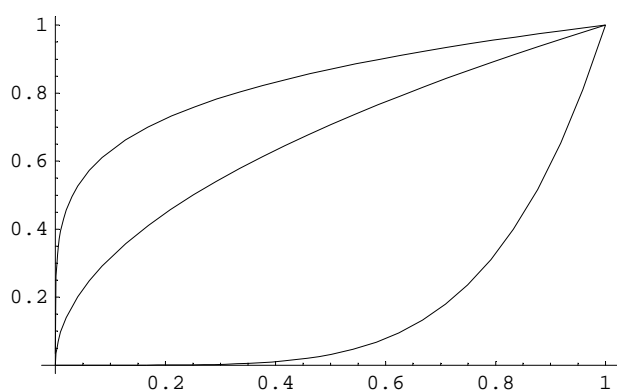
N[%]

{a → 1.37355}

```
Plot[{x^5,x^(1/5),x^1},{x,0,1}];
```

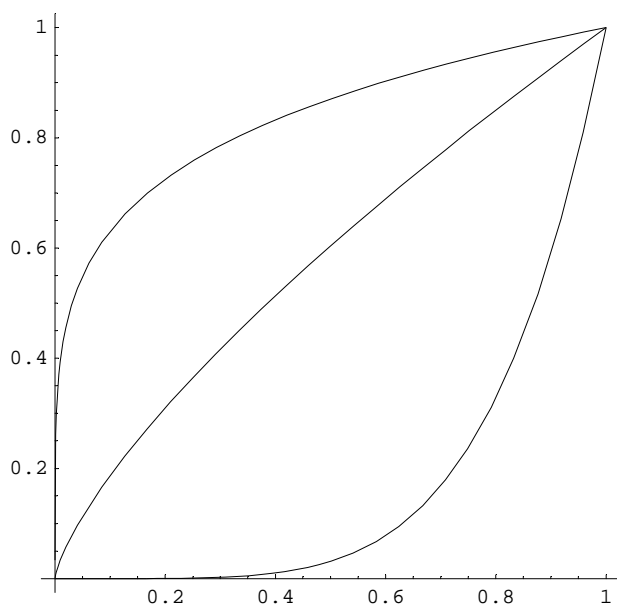


```
Plot[{x^5,x^(1/5),x^(1/2)},{x,0,1}];
```

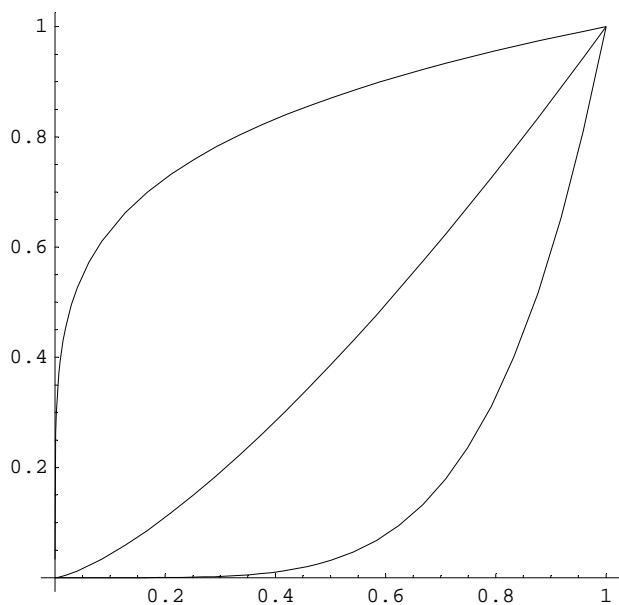


## Plot Goldener Schnitt

```
Plot[Evaluate[{x^5,x^(1/5),x^(a)/.solvl}],{x,0,1},AspectRatio->Automatic];
```



```
Plot[Evaluate[{x^5,x^(1/5),x^(a)/.solv2}],{x,0,1},AspectRatio->Automatic];
```



### 3 Rotationskörper, Parabel

Funktion durch Parabel angenähert. Gleiche Ableitung bei -1 und Werte bei -1 und 1, Winkelabweichung bei 1?

```
f[x_]:= (x^2-1) E^(-x);
p[x_,a_,b_,c_]:= a x^2+b x + c

f'[x]/.x->-1
-2 e

solv=Solve[Evaluate[{p[-1,a,b,c]==0, p[1,a,b,c]==0,
(D[p[x,a,b,c],x]==f'[x]/.x->-1)}]]//Flatten

{a -> e, b -> 0, c -> -e}

%/N
{a -> 2.71828, b -> 0., c -> -2.71828}

p[x_]:= a x^2+b x + c/.solv; p[x]
-e + e x^2

p'[x]/.x->1
2 e

f'[x]/.x->1
2/e

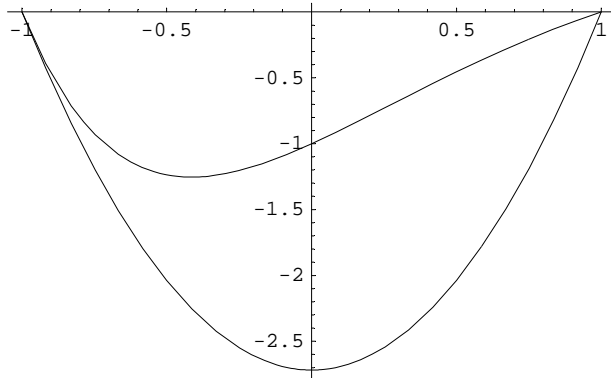
ArcTan[2 E]-ArcTan[2/ E] //N
0.754566
```

```
(ArcTan[2 E]-ArcTan[2/ E]) /Degree//N
```

```
43.2334
```

## a Plot

```
Plot[{f[x],p[x]},{x,-1,1}];
```



## Flächenverhältnis

```
Integrate[(x^2-1) E^(-x),x]
```

```
-e-x (1+x)2
```

```
Integrate[(x^2-1) E^(-x),{x,-1,1}]
```

```
 $-\frac{4}{e}$ 
```

```
%//N
```

```
-1.47152
```

```
Integrate[p[x],x]
```

```
 $-e x + \frac{e x^3}{3}$ 
```

```
Integrate[p[x],{x,-1,1}]
```

```
 $-\frac{4 e}{3}$ 
```

```
%//N
```

```
-3.62438
```

```
int=Integrate[(f[x]-p[x]),{x,-1,1}]/Integrate[(p[x]),{x,-1,1}]
```

```
 $-\frac{3 \left(-\frac{4}{e} + \frac{4 e}{3}\right)}{4 e}$ 
```

```
int//N
```

```
-0.593994
```

```
Integrate[(f[x]),{x,-1,1}]/Integrate[(p[x]),{x,-1,1}]
```

$$\frac{3}{e^2}$$

```
%//N
```

```
0.406006
```

```
1/%//N
```

```
2.46302
```

## Wendepunkt

```
Evaluate[f''[x]]/.x->0
```

```
1
```

```
Solve[Evaluate[f''[x]==0],{x}]
```

```
Solve::ifun : Inverse functions are being used by Solve, so some
solutions may not be found; use Reduce for complete solution information. Mehr...
```

$$\left\{ \left\{ x \rightarrow 2 - \sqrt{3} \right\}, \left\{ x \rightarrow 2 + \sqrt{3} \right\} \right\}$$

```
Solve::ifun : Inverse functions are being used by Solve, so some
solutions may not be found; use Reduce for complete solution information. Mehr...
```

$$\left\{ \left\{ x \rightarrow 2 - \sqrt{3} \right\}, \left\{ x \rightarrow 2 + \sqrt{3} \right\} \right\}$$

```
Solve[Evaluate[f''[x]==0],{x}]/N
```

```
Solve::ifun : Inverse functions are being used by Solve, so some
solutions may not be found; use Reduce for complete solution information. Mehr...
```

$$\left\{ \left\{ x \rightarrow 0.267949 \right\}, \left\{ x \rightarrow 3.73205 \right\} \right\}$$

## Rotationsvolumen bei Parabe, Vergleich mit Zylinder gleicher Länge, r = ? (Hat Volumen in Zylinder mit r=2 Platz?)

```
Pi Integrate[p[x]^2,{x,-1,1}]
```

$$\frac{16 e^2 \pi}{15}$$

```
%//N
```

```
24.761
```

```
Sqrt[Integrate[p[x]^2,{x,-1,1}]/2]
```

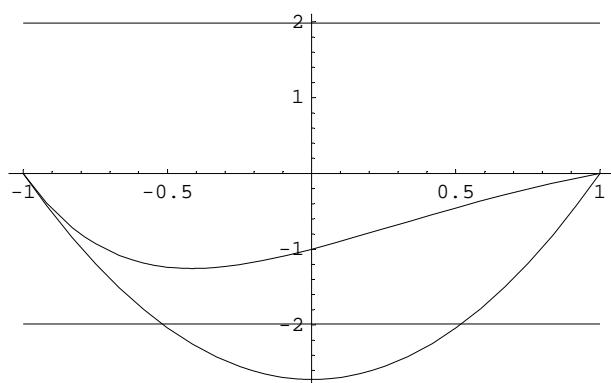
$$2 \sqrt{\frac{2}{15}} e$$

```
%//N
```

```
1.98515
```



```
Plot[{f[x],p[x],-1.9851,1.9851},{x,-1,1}];
```



### Länge der Bögen:

```
{f[x],p[x]}
```

```
{e-x (-1 + x2), -e + e x2}
```

```
l1=NIntegrate[Evaluate[Sqrt[1+D[p[x],x]^2]],{x,-1,1}]
```

```
5.96824
```

```
l2=NIntegrate[Evaluate[Sqrt[1+D[f[x],x]^2]],{x,-1,1}]
```

```
3.37052
```

```
l3=2
```

```
2
```

```
l1/l2
```

```
1.77072
```

```
l1/l3
```

```
2.98412
```

```
l2/l3
```

```
1.68526
```

## 3 Rotationskörper, Parabel mit Punkteverwechslung

Funktion durch Parabel angenähert. Gleiche Ableitung bei -1 und Werte bei -1 und 1, Winkelabweichung bei 1?

```
f[x_]:= (x^2-1) E^(-x);
```

```
p[x_,a_,b_,c_]:= a x^2+b x + c
```

```
f'[x]/.x->1
```

```
 $\frac{2}{e}$ 
```

```
solv=Solve[Evaluate[{p[-1,a,b,c]==0, p[1,a,b,c]==0,
(D[p[x,a,b,c],x]==f'[x]/.x->1)}]]//Flatten
```

$$\left\{c \rightarrow -\frac{1}{e}, a \rightarrow \frac{1}{e}, b \rightarrow 0\right\}$$

```
%//N
```

$$\{c \rightarrow -0.367879, a \rightarrow 0.367879, b \rightarrow 0.\}$$

```
p[x_]:=a x^2+b x + c/.solv; p[x]
```

$$-\frac{1}{e} + \frac{x^2}{e}$$

```
p'[x]/.x->1
```

$$\frac{2}{e}$$

```
f'[x]/.x->1
```

$$\frac{2}{e}$$

```
ArcTan[2 E]-ArcTan[2/ E] //N
```

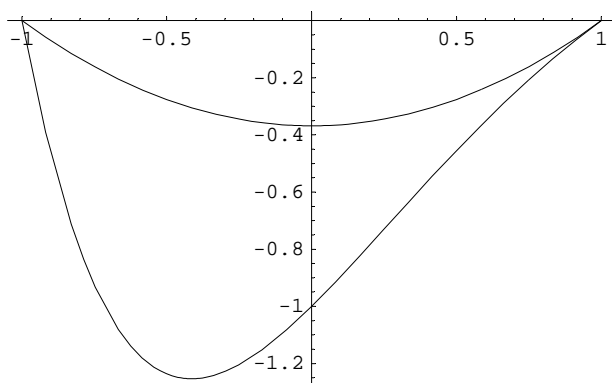
$$0.754566$$

```
(ArcTan[2 E]-ArcTan[2/ E]) /Degree//N
```

$$43.2334$$

## a Plot

```
Plot[{f[x],p[x]},{x,-1,1}];
```



## Flächenverhältnis

```
Integrate[(x^2-1) E^(-x),x]
```

$$-e^{-x} (1+x)^2$$

```
Integrate[(x^2-1) E^(-x),{x,-1,1}]
```

$$-\frac{4}{e}$$

```

%/N
-1.47152

Integrate[p[x],t]

$$\frac{t(-1+x^2)}{e}$$


Integrate[p[x],{x,-1,1}]

$$-\frac{4}{3e}$$


%/N
-0.490506

int=Integrate[(f[x]-p[x]),{x,-1,1}]/Integrate[(p[x]),{x,-1,1}]
2

int//N
2.

Integrate[(f[x]),{x,-1,1}]/Integrate[(p[x]),{x,-1,1}]
3

%/N
3.

1%/N
0.333333

```

## Wendepunkt

```

Evaluate[f''[x]]/.x->0
1

Solve[Evaluate[f''[x]==0],{x}]
Solve::ifun : Inverse functions are being used by Solve, so some
solutions may not be found; use Reduce for complete solution information. Mehr...
{{x -> 2 - Sqrt[3]}, {x -> 2 + Sqrt[3]}}

Solve[Evaluate[f''[x]==0],{x}]/N
Solve::ifun : Inverse functions are being used by Solve, so some
solutions may not be found; use Reduce for complete solution information. Mehr...
{{x -> 0.267949}, {x -> 3.73205}}

```

## Rotationsvolumen bei Parabe, Vergleich mit Zylinder gleicher Länge, r = ? (Hat Volumen in Zylinder mit r=2 Platz?)

```
Pi Integrate[p[x]^2,{x,-1,1}]
```

$$\frac{16 \pi}{15 e^2}$$

```
%//N
```

```
0.453513
```

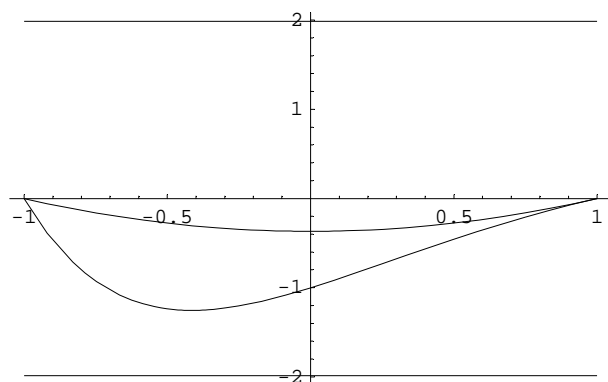
```
Sqrt[Integrate[p[x]^2,{x,-1,1}]/2]
```

$$\frac{2 \sqrt{\frac{2}{15}}}{e}$$

```
%//N
```

```
0.268661
```

```
Plot[{f[x],p[x],-1.9851,1.9851},{x,-1,1}];
```



## Länge der Bögen:

```
{f[x],p[x]}
```

$$\left\{ e^{-x} (-1 + x^2), -\frac{1}{e} + \frac{x^2}{e} \right\}$$

```
l1=NIntegrate[Evaluate[Sqrt[1+D[p[x],x]^2]],{x,-1,1}]
```

```
2.16805
```

```
l2=NIntegrate[Evaluate[Sqrt[1+D[f[x],x]^2]],{x,-1,1}]
```

```
3.37052
```

```
l3=2
```

```
2
```

```
l1/l2
```

```
0.643241
```

11/13

1.08403

12/13

1.68526

## 4 Annäherung Hügel durch Potenzreihe

Funktion durch Parabel angenähert. Gleiche Ableitung bei -1 und Werte bei -1 und 1, Winkelabweichung bei 1?

### Test

```
Remove["Global`*"]
```

```
q[x_,a_,b_,c_,d_,e_] := (a x^2 + b x + c)/(x^2 + d x + e)
```

```
q[x,a,b,c,d,e]//TeXForm
```

```
\frac{a x^2 + b x + c}{x^2 + d x + e}
```

```
sys = {
```

```
q[-2,a,b,c,d,e] == 0,
```

```
q[2,a,b,c,d,e] == 0,
```

```
q[0,a,b,c,d,e] == 2,
```

```
(D[q[x,a,b,c,d,e],x]/.x->1) == -1,
```

```
(D[q[x,a,b,c,d,e],x]/.x->-1) == 1}
```

$$\left\{ \begin{array}{l} \frac{4a - 2b + c}{4 - 2d + e} = 0, \quad \frac{4a + 2b + c}{4 + 2d + e} = 0, \quad \frac{c}{e} = 2, \\ -\frac{(a+b+c)(2+d)}{(1+d+e)^2} + \frac{2a+b}{1+d+e} = -1, \quad -\frac{(a-b+c)(-2+d)}{(1-d+e)^2} + \frac{-2a+b}{1-d+e} = 1 \end{array} \right\}$$

```
solv = Solve[Evaluate[sys, {a,b,c,d,e}]]
```

$$\left\{ \left\{ b \rightarrow 0, c \rightarrow 1, a \rightarrow -\frac{1}{4}, d \rightarrow 0, e \rightarrow \frac{1}{2} \right\}, \right.$$

$$\left. \left\{ b \rightarrow 0, c \rightarrow 8, a \rightarrow -2, d \rightarrow -\sqrt{7}, e \rightarrow 4 \right\}, \left\{ b \rightarrow 0, c \rightarrow 8, a \rightarrow -2, d \rightarrow \sqrt{7}, e \rightarrow 4 \right\} \right\}$$

```
q[x_] := (a x^2 + b x + c)/(x^2 + d x + e) /. solv ; q[x]
```

$$\left\{ \frac{1 - \frac{x^2}{4}}{\frac{1}{2} + x^2}, \frac{8 - 2x^2}{4 - \sqrt{7}x + x^2}, \frac{8 - 2x^2}{4 + \sqrt{7}x + x^2} \right\}$$

### Symmetrie

```
Remove["Global`*"]
```

```
q[x_,a_,c_,e_] := (a x^2 + c)/(x^2 + e)
```

```

sys={
q[2,a,c,e]==0,
q[0,a,c,e]==2,
(D[q[x,a,c,e],x]/.x->1)===-1}

{
 $\frac{4a+c}{4+e} = 0, \frac{c}{e} = 2, -\frac{2(a+c)}{(1+e)^2} + \frac{2a}{1+e} = -1$ 
}

solv=Solve[Evaluate[sys,{a,c,e}]]//Flatten

{c -> 1, a -> - $\frac{1}{4}$ , e ->  $\frac{1}{2}$ }

q[x]:=(a x^2+ c)/(x^2+e)/.solv ; q[x]

 $\frac{1 - \frac{x^2}{4}}{\frac{1}{2} + x^2}$ 

q[x]//Simplify

 $\frac{4 - x^2}{2 + 4 x^2}$ 

```

**Konvergenzbereich: Partialbruchzerlegung, Vergleich mit geometrischer Reihe!**  
**==> r = 1**

```

q1[x]:= Evaluate[q[x]//Apart]; q1[x]

- $\frac{1}{4} + \frac{9}{4(1+2x^2)}$ 

Table[D[q1[x],{x,k}],{k,0,10}]]//Together

{
 $\frac{4-x^2}{2(1+2x^2)}$ , - $\frac{9x}{(1+2x^2)^2}$ ,  $\frac{9(-1+6x^2)}{(1+2x^2)^3}$ , - $\frac{216(-x+2x^3)}{(1+2x^2)^4}$ ,
 $\frac{216(1-20x^2+20x^4)}{(1+2x^2)^5}$ , - $\frac{4320(3x-20x^3+12x^5)}{(1+2x^2)^6}$ ,  $\frac{12960(-1+42x^2-140x^4+56x^6)}{(1+2x^2)^7}$ ,
- $\frac{1451520(-x+14x^3-28x^5+8x^7)}{(1+2x^2)^8}$ ,  $\frac{1451520(1-72x^2+504x^4-672x^6+144x^8)}{(1+2x^2)^9}$ ,
- $\frac{52254720(5x-120x^3+504x^5-480x^7+80x^9)}{(1+2x^2)^{10}}$ ,
 $\frac{261273600(-1+110x^2-1320x^4+3696x^6-2640x^8+352x^{10})}{(1+2x^2)^{11}}$ 
}

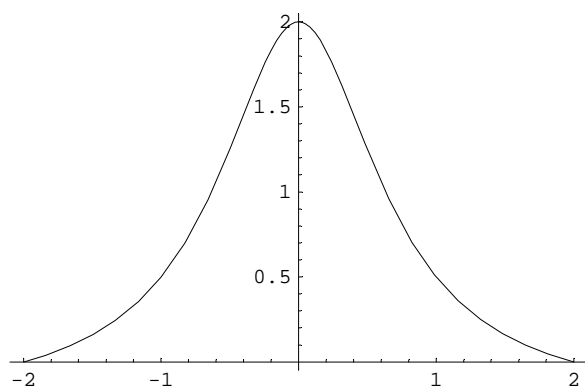
Table[D[q1[x],{x,k}],{k,0,10}]/.x->1.

{0.5, -1., 1.66667, -2.66667, 0.888889,
29.6296, -254.815, 1548.64, -7005.76, 9734.32, 290555.}

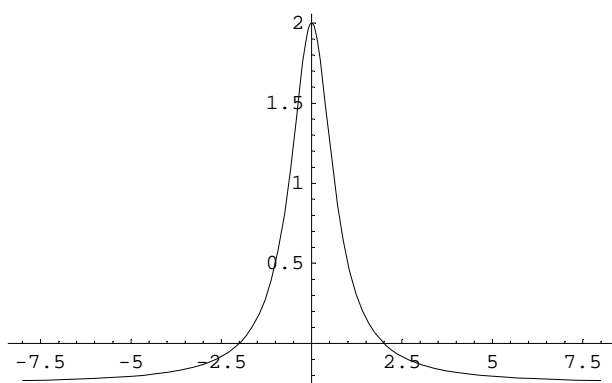
q1[x]:=Evaluate[q[x]]

```

```
Plot[q1[x],{x,-2,2}];
```



```
Plot[q1[x],{x,-8,8}];
```



## Potenzreihe, Abweichung

```
q2[x_]:=Normal[Series[q1[z],{z,0,10}]]/.z->x; q2[x]
```

$$2 - \frac{9x^2}{2} + 9x^4 - 18x^6 + 36x^8 - 72x^{10}$$

```
q2[x_]:=Evaluate[Normal[Series[q1[x],{x,0,10}]]]; q2[x]
```

$$2 - \frac{9x^2}{2} + 9x^4 - 18x^6 + 36x^8 - 72x^{10}$$

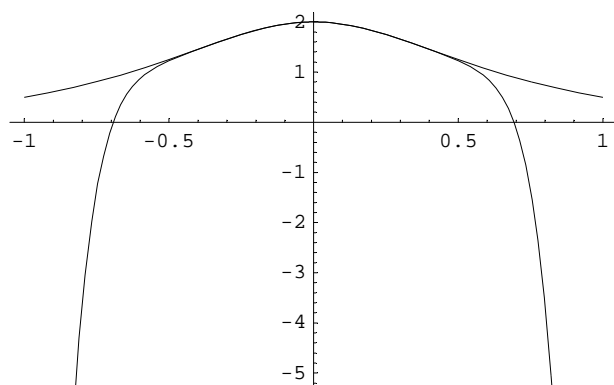
```
{q1[x],q2[x]}
```

$$\left\{ \frac{1 - \frac{x^2}{4}}{\frac{1}{2} + x^2}, 2 - \frac{9x^2}{2} + 9x^4 - 18x^6 + 36x^8 - 72x^{10} \right\}$$

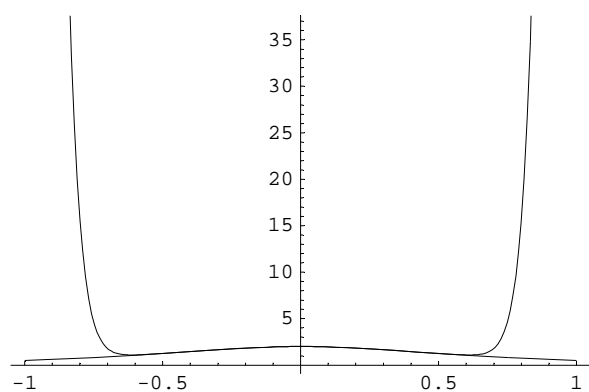
```
{q1[5],q2[5]}/N
```

$$\{-0.205882, -6.89338 \times 10^8\}$$

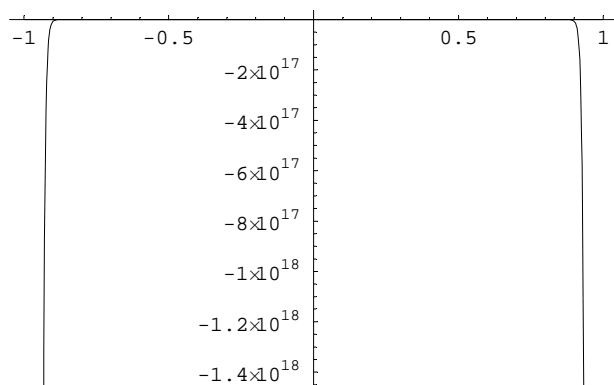
```
Plot[{q1[x],q2[x]},{x,-1,1}];
```



```
q2[x_]:=Evaluate[Normal[Series[q1[x],{x,0,20}]]]; Plot[{q1[x],q2[x]},{x,-1,1}];
```



```
q2[x_]:=Evaluate[Normal[Series[q1[x],{x,0,150}]]]; Plot[{q1[x],q2[x]},{x,-1,1}];
```



```
q2[x_]:=Evaluate[Normal[Series[q1[x],{x,0,10}]]]; d1=q2[x]/.x->0.5
```

1.22656

```
d2=q[x]/.x->0.5
```

1.25

```
d2-d1
```

0.0234375

```
q[x]-q2[x]/.x->0.9
```

15.5228



## 5 Reihe, Maximum Geometrie

**a**

```
Normal[Series[ArcTan[x],{x,0,10}]]
```

$$x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \frac{x^9}{9}$$

```
4(Normal[Series[ArcTan[x],{x,0,10}]]/.x->1)//N
```

3.33968

```
4(Normal[Series[ArcTan[x],{x,0,2000}]]/.x->1)//N
```

3.14059

**b**

10m : 2m

Breite 10 m

Höhe:  $x : 2 = (x+10) : h$ ,  $l = f[x]$

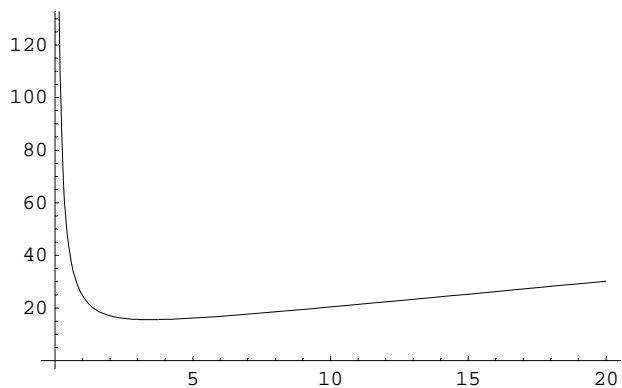
```
Solve[ x / 2 == (x+10) / h, {h}]
```

$$\left\{ \left\{ h \rightarrow \frac{2(10+x)}{x} \right\} \right\}$$

```
f[x_] := Sqrt[ ( (2(10+x)/x) ^ 2 + (x+10) ^ 2 ); f[x]
```

$$\sqrt{(10+x)^2 + \frac{4(10+x)^2}{x^2}}$$

```
Plot[f[x],{x,0,20}];
```



**f' [x]**

$$\frac{2(10+x) + \frac{8(10+x)}{x^2} - \frac{8(10+x)^2}{x^3}}{2\sqrt{(10+x)^2 + \frac{4(10+x)^2}{x^2}}}$$

**Solve[Evaluate[f'[x]==0],{x}]**

{x → -2 (-5)<sup>1/3</sup>, {x → 2 5<sup>1/3</sup>, {x → 2 (-1)<sup>2/3</sup> 5<sup>1/3</sup>}

**Solve[Evaluate[f'[x]==0],{x}]/N**

{x → -1.70998 - 2.96177 i}, {x → 3.41995}, {x → -1.70998 + 2.96177 i}}

**(-5)<sup>1/3</sup> // N**

0.854988 + 1.48088 i

**(-1)<sup>2/3</sup> // N**

-0.5 + 0.866025 i

**((-1)<sup>2/3</sup>)<sup>2</sup> // N**

-0.5 - 0.866025 i

**((-1)<sup>2/3</sup>)<sup>3</sup> // N**

1.

**C**

**tan1=49/10**

$$\frac{49}{10}$$

**weite=2/tan1 -0.7**

-0.291837