

Kurs ■ Cours

14. Input und Output ■ Input et output

Die Gliederung dieses Kurses folgt in groben Zügen dem Buch von Nancy Blachman: *A Practical Approach*.... Hinweis: Kapitel 14 lesen!

- L'articulation de ce cours correspond à peu près à celle du livre de Nancy Blachman: *A Practical Approach*....
Indication: Lire le chapitre 14.

Run mit WIN+*Mathematica* Version 5.2

- Testé avec *Mathematica* version 5.2+WIN

WIR94/98/99/2000/2007 // Copyright Rolf Wirz

Problem: Datenimport und Datenexport in und von *Mathematica*.

- Problème: Importation et exportation de données dans et de *Mathematica*.

14.1. Input ■ Input

14.1.1. Dateneingabe via Tastatur während des Programmmlauf

- Entrée des données par les touches pendant que le programme marche

Studiere: ■ Etudie:

`In[1]:= ?Input`

`Input[]` interactively reads in one *Mathematica* expression.

`Input["prompt"]` requests input, using the specified string as a prompt. Mehr...

`In[2]:= ?InputString`

`InputString[]` interactively reads in a character string.

`InputString["prompt"]` requests input, using the specified string as a prompt. Mehr...

```
In[3]:= ?BaseForm
```

BaseForm[expr, n] prints with the numbers in expr given in base n. Mehr...

```
In[4]:= BaseForm[15,2]+BaseForm[17,2]
```

```
Out[4]= 11112 + 100012
```

```
In[5]:= benutzerInput = Input[
  "Schreibe eine Zahl zwischen 1 und 10: \
  Ecris un nombre entre 1 et 10:"]
```

```
Out[5]= 8
```

Achtung: Das nachfolgende Programm bricht erst ab, wenn keine Integer-Zahl eingegeben wird! Probiere:

■ Attention: Le programme suivant s'interrompt seulement si on n'entre pas le nombre Integer! Essaie:

```
In[6]:= dualUmwandlung:=
  Module[{benutzerInput},
    While[
      IntegerQ[
        userInput = Input[
          "Schreibe eine Zahl zwischen 1 und 10: \
          Ecris un nombre entre 1 et 10:"]
        ],
      Print[userInput, " = ",
        BaseForm[userInput, 2]]
    ]
  ];
```

dualUmwandlung

1 = 1₂

2 = 10₂

3 = 11₂

4 = 100₂

5 = 101₂

6 = 110₂

7 = 111₂

8 = 1000₂

9 = 1001₂

(* Input ==> 0.1 !!! *)

```
In[8]:=
```

14.1.2. Datenimport von einem File

■ Importation de données d'un fichier

Achtung: Achte auf das zu deinem Betriebssystem lauffähige Beispiel!

Der Umgang mit externen Dateien von *Mathematica* aus hat ab Version 3.0 eine

grosse Veränderung erfahren!

■ **Attention: Prends seulement les exemples qui tournent sur ton propre système!**
Le traitement des fichiers externes depuis *Mathematica* a beaucoup changé depuis la version 3.0!

Beispiel:

(Das File AAAdaten) befindet sich wahrscheinlich in Deinem Verzeichnis C:\Programme\WolframResearch\Mathematica\3.0 (win98). - Sonst musst Du Deinen mir nicht bekannten Pfad suchen!)

■ Exemple:

(Le file AAAdaten.nb (aadata.ma) se trouve probablement dans le repertoire C:\Programme\WolframResearch\Mathematica\3.0 (win98). - Si non tu dois chercher ton "path" que je ne connais pas!)

Mathematica 3.02, Windows98

Beispiel: neues Verzeichnis erstellen:

■ Faire un nouveau repertoire:

```
In[239]:=
```

```
CreateDirectory["C:\work\MathematicaData\NewDir"]
```

```
Out[239]=
```

```
C:\work\MathematicaData\NewDir
```

```
In[9]:= x = Sin[3] // N >> AAAdaten
```

```
In[10]:= << AAAdaten
```

```
Out[10]= 0.14112
```

Beispiel: Erstelle ein Verzeichnis C:\work (falls nicht vorhanden).

(Das File AABDaten befindet sich in Deinem Verzeichnis "work" (win98), (aadata.ma: "Mate" (win3.1, 95...), "WirzMathematicaFiles/Daten" (NeXT) usw.) . - Sonst musst Du Deinen mir nicht bekannten Pfad angeben!)

■ Exemple: Ouvre un repertoire C:\work (si cela n'existe pas encore).

(Le file AABDaten se trouve dans le repertoire "work" (win98), (aadata.ma: "Mate" (win3.1, 95...), "WirzMathematicaFiles/Daten" (NeXT) etc.). - Si non tu dois m'indiquer ton "path" que je ne connais pas!)

Schreibe Daten ins File C:\work\AABDaten:

■ Ecrire des données dans le fichier C:\work\AABDaten:

```
In[11]:= "3 4 5 1 2 3 6 6.3 7.8 4 r s t hallo
          7777 6666 4.321 1.11111, {1,2,3,4}" >>
          C:\work\MathematicaData\AABDaten;
```

```
In[12]:= {"Cos[3]//N", Cos[3] // N} >> C:\work\MathematicaData\AACDaten;
```

```
In[13]:= {3 4 5 1 2 3 6 6, "3 4 5 1 2 3 6 6",
          {3 4 5 1 2 3 6 6}} >> C:\work\MathematicaData\AACDaten;
```

Lese das File C:\work\AABDaten:

■ Lire le fichier C:\work\AABDaten:

```
In[14]:= << C:\work\MathematicaData\AABDaten
```

```
Out[14]= 3 4 5 1 2 3 6 6.3 7.8 4 r s t hallo 7777 6666 4.321 1.11111, {1,2,3,4}
```

```
In[15]:= !! C:\work\MathematicaData\AABDaten
          "3 4 5 1 2 3 6 6.3 7.8 4 r s t hallo 7777 6666 4.321 1.11111, {1,2,3,4}"
```

win98:

Erstelle nötigenfalles eine Textdatei "c:\work\AAEDaten.txt" mit Inhalt:

■ Si nécessaire composer un fichier "c:\work\AAEDaten.txt" avec le contenu:

```
1 2 3 4 5 6 7
1.1 1.2 1.3 1.4
11 12 13 14 115
a b c d e f g
Sin[5]\N hallo
"hallo"
```

Erstelle ebenso eine Textdatei "c:\work\AAFdaten.txt" mit Inhalt:

■ Composer aussi un fichier "c:\work\AAEDaten.txt" avec le contenu:

```
1 2 3 4 5 6 7
1.1 1.2 1.3 1.4
11 12 13 14 115
```

Inhalt anschauen:

■ Regarder le contenu:

```
In[16]:= !! "C:\work\MathematicaData\AAFdaten.txt"
          1234 k341jök4j8sn3i 43 45 dkr kjkj
          fjkldjklf
          12345
          677890
```

```
In[17]:= (* !!f:\Mathe/Daten/aadaten0 (* win3.1 etc. *) *)
```

File einlesen und ausführen:

■ Lire le fichier et exécuter:

```
In[18]:= << C:\work\MathematicaData\AAFdaten.txt
```

```
Out[18]= 677890
```

```
In[19]:= (* <<f:\Mathe/Daten/aadaten1 (* win3.1 etc. *) *)
```

Was ist los gewesen? Schauen wir weiter:

■ Que s'est-il passé? Continuons d'observer:

```
In[20]:= ?<<
```

```
<<name reads in a file, evaluating each expression in it, and returning the last one. Mehr...
```

```
In[21]:= ?Get
```

```
<<name reads in a file, evaluating each expression in it, and returning the last one. Mehr...
```

```
In[22]:= !!C:\\work\\MathematicaData\\AAEDaten.txt
```

```
1234 99 2 3 4 5 11 1.2 1.12334455
1.123344335
12345
677890
```

```
In[23]:= (* !!f:\Mathe/Daten/aadaten1 (* win3.1 etc. *) *)
```

```
In[24]:= << C:\\work\\MathematicaData\\AAEDaten.txt
```

```
Out[24]= 677890
```

```
In[25]:= (* <<f:\Mathe/Daten/aadaten1 (* win3.1 etc. *) *)
```

```
In[26]:= Get["C:\\work\\MathematicaData\\AAEDaten.txt"]
```

```
Out[26]= 677890
```

```
In[27]:= (* Get["f:\Mathe/Daten/aadaten1"]
           (* win3.1 etc. *) *)
```

```
In[28]:= 1 7 3 4 2 9 (*Produkt! *)
```

```
Out[28]= 1512
```

Spezifisch einlesen:

■ Lire spécifiquement:

```
In[29]:= ?ReadList
```

ReadList["file"] reads all the remaining expressions in a file, and returns a list of them. ReadList["file", type] reads objects of the specified type from a file, until the end of the file is reached. The list of objects read is returned. ReadList["file", {type1, type2, ...}] reads objects with a sequence of types, until the end of the file is reached. ReadList["file", types, n] reads only the first n objects of the specified types. Mehr...

```
In[31]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt", Real]
```

```
Out[31]= {1234., 99., 2., 3., 4., 5., 11., 1.2, 1.12334, 1.12334, 12345., 677890.}
```

```
In[32]:= (* ReadList["f:\Mathe/Daten/aadaten0", Real] *)
           (* win3.1 etc. *)
```

```
In[34]:= ?Real
```

Real is the head used for real (floating-point) numbers. Mehr...

```
In[35]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt", Number]
```

```
Out[35]= {1234, 99, 2, 3, 4, 5, 11, 1.2, 1.12334, 1.12334, 12345, 677890}
```

```
In[36]:= (* ReadList["f:\Mathe/Daten/aadaten0", Number] *)
           (* win3.1 etc. *)
```

```
In[38]:= ?Number
```

Number represents an exact integer or an approximate real number in Read. Mehr...

```
In[39]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", Byte]
```

```
Out[39]= {49, 50, 51, 52, 32, 32, 107, 51, 52, 108, 106, 246, 107, 52, 106,
          56, 115, 110, 51, 105, 32, 52, 51, 32, 52, 53, 32, 100, 107, 114, 32,
          107, 106, 107, 106, 10, 102, 106, 107, 108, 100, 106, 107, 108, 102,
          32, 10, 49, 50, 51, 52, 53, 10, 54, 55, 55, 56, 57, 48, 10, 32, 32, 32}
```

```
In[40]:= (* ReadList["f:\\Mathe/Daten/aadaten0", Byte] *)
          (* win3.1 etc. *)
```

```
In[42]:= ?Byte
```

Byte represents a single byte of data in Read. Mehr...

```
In[43]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", Character]
```

```
Out[43]= {1, 2, 3, 4, , , k, 3, 4, 1, j, ö, k, 4, j, 8,
          s, n, 3, i, , 4, 3, , 4, 5, , d, k, r, , k, j, k, j,
          , f, j, k, l, d, j, k, l, f, ,
          , 1, 2, 3, 4, 5,
          , 6, 7, 7, 8, 9, 0,
          , , , }
```

```
In[44]:= (* ReadList["f:\\Mathe/Daten/aadaten0",
                  Character] (* win3.1 etc. *) *)
```

```
In[45]:= ?Character
```

Character represents a single character in Read. Mehr...

```
In[46]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", String]
```

```
Out[46]= {1234 k34ljök4j8sn3i 43 45 dkr kjkj, fjkldjklf , 12345, 677890, }
```

```
In[47]:= (* ReadList["f:\\Mathe/Daten/aadaten0", String]
          (* win3.1 etc. *) *)
```

```
In[48]:= ?String
```

String is the head of a character string "text". Mehr...

```
In[49]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", Record]
```

```
Out[49]= {1234 k34ljök4j8sn3i 43 45 dkr kjkj, fjkldjklf , 12345, 677890, }
```

```
In[50]:= (* ReadList["f:\\Mathe/Daten/aadaten0", Record] *)
          (* win3.1 etc. *)
```

```
In[52]:= ?Record
```

Record represents a record in Read, Find and related functions. Mehr...

```
In[53]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", Word]
```

```
Out[53]= {1234, k34ljök4j8sn3i, 43, 45, dkr, kjkj, fjkldjklf, 12345, 677890}
```

```
In[54]:= (* ReadList["f:\\Mathe/Daten/aadaten0", Word] *)
          (* win3.1 etc. *)
```

```
In[56]:= ?Word
```

Word represents a word in Read, Find and related functions. Mehr...

```

In[57]:= (* ReadList["f:\Mathe/Daten/aadaten1", Real] *)
          (* win3.1 etc. *)

In[59]:= (* ReadList["f:\Mathe/Daten/aadaten1", Number] *)
          (* win3.1 etc. *)

In[61]:= (* ReadList["f:\Mathe/Daten/aadaten2", Number] *)
          (* win3.1 etc. *)

In[63]:= (* !!f:\Mathe/Daten/aadaten2      (* win3.1 etc. *) *)

In[64]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt", {Number, Number}]
Out[64]= {{1234, 99}, {2, 3}, {4, 5}, {11, 1.2}, {1.12334, 1.12334}, {12345, 677890}}

In[65]:= (* ReadList["f:\Mathe/Daten/aadaten1",
                    {Number, Number}] *)      (* win3.1 etc. *)

In[66]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt",
                    {Number, Number, Number, Number}]
Out[66]= {{1234, 99, 2, 3}, {4, 5, 11, 1.2}, {1.12334, 1.12334, 12345, 677890}}

In[67]:= (* ReadList["f:\Mathe/Daten/aadaten1",
                    {Number, Number, Number, Number}] *)
          (* win3.1 etc. *)

In[69]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt", Cos[Number]]
Out[69]= {Cos[1234], Cos[99], Cos[2], Cos[3], Cos[4], Cos[5],
          Cos[11], 0.362358, 0.43267, 0.43267, Cos[12345], Cos[677890]}

In[70]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt", Cos[Number]] // N
Out[70]= {-0.798551, 0.0398209, -0.416147, -0.989992, -0.653644,
          0.283662, 0.0044257, 0.362358, 0.43267, 0.43267, 0.111436, -0.961386}

In[71]:= (* ReadList["f:\Mathe/Daten/aadaten1",
                    Cos[Number]] *)          (* win3.1 etc. *)

In[72]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", Cos[Number]] // N
          Read::readn : Syntax error reading a real number from C:\work\MathematicaData\AAFDaten.txt. Mehr...
Out[72]= {-0.798551}

In[73]:= (* ReadList["f:\Mathe/Daten/aadaten1",
                    Cos[Number]] // N *)      (* win3.1 etc. *)

In[74]:= (* !!f:\Mathe/Daten/aadaten3 *)     (* win3.1 etc. *)

In[75]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt",
                    {String, Number, Number}]
          Read::readn : Syntax error reading a real number from C:\work\MathematicaData\AAFDaten.txt. Mehr...
Out[75]= {{1234 k341ljök4j8sn3i 43 45 dkr kjkj, $Failed, EndOfFile}}

In[76]:= (* ReadList["f:\Mathe/Daten/aadaten3",
                    {String, Number, Number}] *)      (* win3.1 etc. *)

In[77]:= (* !!f:\Mathe/Daten/aadaten4 *)     (* win3.1 etc. *)

```

```
In[78]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt",
  {Number, Number, String}]
```

Read::readn : Syntax error reading a real number from C:\work\MathematicaData\AAFDaten.txt. Mehr...

```
Out[78]= {{1234, $Failed, EndOfFile}}
```

```
In[79]:= (*ReadList["f:\Mathe/Daten/aadaten4",
  {Number, Number, String}] *) (* win3.1 etc. *)
```

```
In[80]:= (*!!f:\Mathe/Daten/aadaten5 *) (* win3.1 etc. *)
```

```
In[81]:= (* ReadList["f:\Mathe/Daten/aadaten5",
  {Number, Number, String}] *) (* win3.1 etc. *)
```

Probiere eigene files!

■ Essaie tes propres fichiers!

14.1.3. Einlesen von Records und Words

■ Lire Records et Words

Studiere die "Befehle":

■ Etudie les "ordres":

```
In[82]:= ?*Record*
```

System`

```
NullRecords RecordLists
Record RecordSeparators
```

```
In[83]:= ?RecordLists
```

RecordLists is an option for ReadList which specifies whether objects from separate records should be returned in separate sublists. Mehr...

```
In[84]:= ?RecordSeparators
```

RecordSeparators is an option for Read, Find and related functions which specifies the list of strings to be taken as delimiters for records. Mehr...

```
In[85]:= ?WordSeparators
```

WordSeparators is an option for Read, Find and related functions which specifies the list of strings to be taken as delimiters for words. Mehr...

```
In[86]:= ?NullRecords
```

NullRecords is an option for Read and related functions which specifies whether null records should be taken to exist between repeated record separators. Mehr...

```
In[87]:= ?NullWords
```

NullWords is an option for Read and related functions which specifies whether null words should be taken to exist between repeated word separators. Mehr...


```
In[88]:= ?TokenWords
```

TokenWords is an option for Read and related functions
which gives a list of token words to be used to delimit words. Mehr...

Studiere die Anwendungen:

■ Etudie les applications:

```
In[89]:= !!C:\\work\\MathematicaData\\AABDaten
```

```
"3 4 5 1 2 3 6 6.3 7.8 4 r s t hallo 7777 6666 4.321 1.11111, {1,2,3,4}"
```

```
In[90]:= !!C:\\work\\MathematicaData\\AAGDaten.txt
```

```
asdf 5 34 dkfjke jkdf
```

```
In[91]:= (* !!f:\\Mathe/Daten/spsheet0 *) (* win3.1 etc. *)
```

```
In[92]:= ReadList["C:\\work\\MathematicaData\\AAEDaten.txt",  
{Number, Number, Number}]
```

```
Out[92]= {{1234, 99, 2}, {3, 4, 5}, {11, 1.2, 1.12334}, {1.12334, 12345, 677890}}
```

```
In[93]:= (* ReadList["f:\\Mathe/Daten/spsheet0",  
{Number, Number, Number}] *) (* win3.1 etc. *)
```

```
In[94]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt",  
Word, RecordLists -> True]
```

```
Out[94]= {{1234, k341jök4j8sn3i, 43, 45, dkr, kjkj}, {fjkl djklf}, {12345}, {677890}}
```

```
In[95]:= (*ReadList["f:\\Mathe/Daten/spsheet0",  
Word, RecordLists ->True] *) (* win3.1 etc. *)
```

```
In[96]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt", Word]
```

```
Out[96]= {1234, k341jök4j8sn3i, 43, 45, dkr, kjkj, fjkl djklf, 12345, 677890}
```

```
In[97]:= (* ReadList["f:\\Mathe/Daten/spsheet0",  
Word] *) (* win3.1 etc. *)
```

```
In[98]:= ReadList["C:\\work\\MathematicaData\\AAFDaten.txt",  
RecordLists -> True]
```

```
Out[98]= {{2387790 dkr k341jök4j8sn3i kjkj}, {fjkl djklf}, {12345}, {677890}, {Null}}
```

```
In[99]:= (* ReadList["f:\\Mathe/Daten/spsheet0",  
RecordLists ->True] *) (* win3.1 etc. *)
```

```
In[100]:=
```

```
Clear[x];  
(* x = ReadList["f:\\Mathe/Daten/spsheet0",  
Word,  
WordSeparators -> {"\t"},  
RecordLists ->True] *) (* win3.1 etc. *)
```

```
In[102]:=
Clear[x];
x = ReadList["C:\\work\\MathematicaData\\AAGDaten.txt",
            Word,
            WordSeparators -> {"\t"},
            RecordLists -> True]
```

```
Out[103]=
{{asdf 5 34 dkfjke jkdf}, {  }}
```

```
In[104]:=
?Word

Word represents a word in Read, Find and related functions. Mehr...
```

```
In[105]:=
ToExpression[x]
```

```
Out[105]=
{{170 asdf dkfjke jkdf}, {Null}}
```

```
In[106]:=
?ToExpression

ToExpression[input] gives the expression obtained by interpreting strings
or boxes as Mathematica input. ToExpression[input, form] uses interpretation
rules corresponding to the specified form. ToExpression[input, form, h]
wraps the head h around the expression produced before evaluating it. Mehr...
```

```
In[107]:=
FullForm[x]
```

```
Out[107]//FullForm=
List[List["asdf 5 34 dkfjke jkdf"], List["  "]]
```

```
In[108]:=
(* ReadList["f:\Mathe/Daten/spsheet1",
            {Word, Number, Number, Number},
            WordSeparators -> {" "},
            RecordLists ->True] *) (* win3.1 etc. *)
```

```
In[109]:=
ReadList["C:\\work\\MathematicaData\\AAGDaten.txt",
        {Word, Number, Number, Number},
        WordSeparators -> {" "},
        RecordLists -> True]
```

Read::readn : Syntax error reading a real number from C:\\work\\MathematicaData\\AAGDaten.txt. Mehr...

```
Out[109]=
{{{asdf, 5, 34, $Failed}}}
```

```
In[110]:=
FullForm[%]
```

```
Out[110]//FullForm=
List[List[List["asdf", 5, 34, $Failed]]]
```

14.1.3. Ein längeres Beispiel ■ Un exemple plus long

Zuerst definieren wir Funktionen. Damit können wir obigen Befehl "nachbilden":

■ D'abord nous définissons des fonctions. Avec cela nous pouvons "imiter" l'ordre ci-dessus.

```
In[111]:=
Clear[tabSeparate, tabSep];
tabSeparate[str_String]:= Apply[tabSep,
  Characters[str]];
tabSep[x__String, "\t", y__String]:=
  Flatten[{tabSep[x], tabSep[y]}, 1];
tabSep[x__String]:=
  ToExpression[StringJoin[x]]/;
  FreeQ[{x}, "\t"];
ReadList["C:\\work\\MathematicaData\\AAGDaten.txt",
  tabSeparate[String]]
```

```
Out[115]=
{170 asdf dkfjke jkdf, Null}
```

```
In[116]:=
(*Clear[tabSeparate, tabSep];
tabSeparate[str_String]:=Apply[tabSep,
  Characters[str]];
tabSep[x__String, "\t", y__String]:=
  Flatten[{tabSep[x], tabSep[y]}, 1];
tabSep[x__String]:=
  ToExpression[StringJoin[x]]/;
  FreeQ[{x}, "\t"];
ReadList["f:\Mathe/Daten/spsheet1",
  tabSeparate[String]](* win3.1 etc. *)*)
```

```
In[117]:=
?Characters

Characters["string"] gives a list of the characters in a string. Mehr...
```

```
In[118]:=
?FreeQ

FreeQ[expr, form] yields True if no subexpression in expr
matches form, and yields False otherwise. FreeQ[expr, form, levelspec]
tests only those parts of expr on levels specified by levelspec. Mehr...
```

Achtung! *Mathematica* ist nicht für Datamanagement und Datamanipulation gebaut. Man kann Daten in speziellen Datamanagement-Sprachen oder Programmen (low-level- Programmierung) viel schneller parsen (einlesen und interpretieren) sowie manipulieren. Dies ist bei grösseren Datenmengen wesentlich. Man denke z. B. an (1000 x 1000)-Matrizen in der Statistik, z.B. bei 1000 Beobachtungen von 1000 Variablen.

■ Attention: *Mathematica* n'est pas conçu pour le "management" ni pour la manipulation des données. On peut lire et interpréter ("parser") de même que manipuler beaucoup plus rapidement les données à l'aide de langages "datamanagement" ou programmes (programmation low-level). Cela est essentiel pour des quantités plus importantes de données. On pense p.ex. aux matrices (1000 x 1000) dans la statistique, p.ex. 1000 observations de 1000 variables.

14.1.4. Externe Kommandos bis exklusive Version 3.0 (für WIN98 nicht zu empfehlen)

■ Commandements extérieurs jusqu'à version 3.0, exclusive (pour WIN98 pas recommandé)

Mit "!"Kommando" kann ein externes Kommando ausgeführt werden. Leider haben wir auf NeXT keinen ModulaII-Compiler oder Java-Compiler, so dass wir selbst solche Kommandos bauen könnten. Eine andere Programmiersprache, die den Zweck erfüllen würde, wird an der Schule momentan nicht unterrichtet. Hier ist für NeXT das Programm "aa_ascii", das Umlaute in TeX-Format übersetzt. Studiere das Beispiel:

■ Par "commandement !" on peut exécuter un commandement extérieur. Malheureusement nous n'avons pas de compilateur pour ModulaII ou Java sur NeXT pour pouvoir construire de tels commandements. Une autre langue de programmation qui serve pour le même but n'est actuellement pas enseigné à cette école. Ici on utilise pour NeXT le programme "aa_ascii" qui transforme les "Umlaute" (métaphonie, voyelle infléchie) de l'allemand dans le format TeX. Etudie l'exemple:

```
In[119]:=
      !!C:\\work\\MathematicaData\\AABDaten
      "3 4 5 1 2 3 6 6.3 7.8 4 r s t hallo 7777 6666 4.321 1.11111, {1,2,3,4}"

In[120]:=
      (* !!f:\\Mathe\\Daten\\spsheet2 *)

In[121]:=
      !C:\\work\\MathematicaData\\AABDaten

In[122]:=
      (* !f:\\Mathe\\Daten\\aa_ascii
         f:\\Mathe\\Daten\\spsheet2
         f:\\Mathe\\Daten\\tex -tex;
      ReadList["f:\\Mathe\\Daten\\tex",
              {Word, Number, Number, Number},
              WordSeparators -> {" "},
              RecordLists ->True] *)
```

Das "!"Kommando" kann auch in ReadList stehen, falls es sich auf eine Operation auf einem File bezieht (und nicht zwei Files aufruft)! Folgendes geht nicht:

■ Le "commandement !" peut se trouver aussi dans ReadList, s'il se rapporte à une opération sur un fichier (et n'appelle pas deux fichiers)! La chose suivante ne va pas:

```
In[123]:=
      (* ReadList["!f:\\Mathe\\Daten\\aa_ascii
         f:\\Mathe\\Daten\\spsheet2
         f:\\Mathe\\Daten\\tex -tex ",
              {Word, Number, Number, Number},
              WordSeparators -> {" "},
              RecordLists ->True] *)
```

Externe Kommandos ab Version 3.0

■ Commandements extérieurs à partir de version 3.0

Verwendung externer Programme für Datenmanipulationen von *Mathematica* aus mit Hilfe der Befehle "Install", "Links", "MLPut...", "MLGet...", u.s.w.

Momentan sind keine Programme vorhanden, die problemlos auf irgendwelchen hier unbekanntenen Systemen laufen. Daher wird auf ein konkretes Beispiel verzichtet. Probiere daher mit eigenen Programmen.

■ Utiliser des Programmes externes pour manipuler des données depuis *Mathematica* à l'aide des ordres "Install", "Links", "MLPut...", "MLGet...", etc.

Dans ce moment nous n'avons pas de programmes qui tournent sans problèmes sur n'importe quel système inconnu chez nous. C'est pourquoi nous renonçons à présenter un exemple concret. Essaie avec tes propres programmes.

14.2. Datenexport

■ Exportation de données

14.2.1. Zeichenweise in ein File schreiben

■ Ecrire les signes l'un après l'autre dans un fichier

Beispiel

■ Exemple

Zuerst Daten erzeugen, die exportiert werden sollen:

■ D'abord générer les données qui doivent être exportées:

```
In[124]:=
Clear[daten];
daten = Table[Random[Integer,{1,9}],{2},{6}]
```

```
Out[125]=
{{3, 1, 3, 2, 2, 3}, {9, 2, 2, 3, 3, 4}}
```

Studiere die Befehle:

■ Etudie les ordres:

```
In[126]:=
?>>

expr >> filename writes expr to a file. Put[expr1,
expr2, ... , "filename"] writes a sequence of expressions expr1 to a file. Mehr...
```

```
In[127]:=
?Put

expr >> filename writes expr to a file. Put[expr1,
expr2, ... , "filename"] writes a sequence of expressions expr1 to a file. Mehr...
```

```

In[128]:=
  ??WriteString

  WriteString[channel, expr1, expr2, ... ] converts the expr1 to strings,
    and then writes them in sequence to the specified output channel. Mehr...

  Attributes[WriteString] = {Protected}

In[129]:=
  ?OpenWrite

  OpenWrite["file"] opens a file to write output to it, and returns an OutputStream object.
  Mehr...

In[130]:=
  ?Close

  Close[stream] closes a stream. Mehr...

In[131]:=
  ?Scan

  Scan[f, expr] evaluates f applied to each element of expr in turn. Scan[f,
    expr, levelspec] applies f to parts of expr specified by levelspec. Mehr...

In[132]:=
  ?Rest

  Rest[expr] gives expr with the first element removed. Mehr...

```

Zum Exportieren wollen wir eine Funktion definieren, die die Generierte in der Art Matrix "Zeilenvektor auf Zeile ... (Record) im File" schreibt:

■ Nous allons définir une fonction pour exporter, qui écrit la générée dans la matrice dans le sens "vecteur de ligne sur ligne (Record) dans le fichier":

```

In[133]:=
  Remove[schreibMatrix];
  Off[neufile];
  schreibMatrix[fileName_String, data_List] :=
    Block[{neufile = OpenWrite[fileName]},
      Scan[(WriteString[neufile, First[#]];
        Scan[WriteString[neufile,
          "\t", #]&, Rest[#]]];
        WriteString[neufile, "\n"]]&,
        data];
      Close[neufile]];

In[136]:=
  daten = {{1, 2}, {3, 4, 5, 6}, {7, 8, 9, 10, a}, {b}}

Out[136]=
  {{1, 2}, {3, 4, 5, 6}, {7, 8, 9, 10, a}, {b}}

In[137]:=
  schreibMatrix["C:\\work\\MathematicaData\\AAHDaten", daten]

Out[137]=
  C:\work\MathematicaData\AAHDaten

In[138]:=
  (* schreibMatrix["f:\Mathe/Daten/neuDaten", daten] (* win3.1 etc. *) *)

```

```

In[139]:=
  !! "C:\\work\\MathematicaData\\AAHDaten"

  1  2
  3  4  5  6
  7  8  9  10  a
  b

In[140]:=
  (* !!f:\Mathe/Daten/neuDaten *) (* win3.1 etc. *)

In[141]:=
  ?schreibMatrix

Global`schreibMatrix

schreibMatrix[fileName_String, data_List] :=
  Block[{neufile = OpenWrite[fileName]}, Scan[(WriteString[neufile, First[#1]];
    Scan[WriteString[neufile, #1] &, Rest[#1]]; WriteString[neufile,
  ] &, data]; Close[neufile]]

```

14.2.2. Abspeichern von Definitionen

■ Mémoriser des définitions

Beispiel

■ Exemple

Studiere: ■ Etudie:

```

In[142]:=
  ?Save

Save["filename", symbol] appends definitions associated with the specified symbol to a
file. Save["filename", "form"] appends definitions associated with all symbols
whose names match the string pattern form. Save["filename", "context"] appends
definitions associated with all symbols in the specified context. Save["filename",
{object1, object2, ...}] appends definitions associated with several objects. Mehr...

```

```

In[143]:=
  f[x_] := Sin[x^2] / (E^(-x) Cos[x]);
  Save["C:\\work\\MathematicaData\\AA_f", f]

```

```

In[145]:=
  (* f[x_] := Sin[x^2]/(E^(-x) Cos[x]);
  Save["f:\Mathe/Daten/AAA_f", f]
  (* win3.1 etc. *) *)

```

```

In[146]:=
  !! C:\\work\\MathematicaData\\AA_f

f[x_] := Sin[x^2]/(Cos[x]/E^x)

x = {"dddt ejkrjke dfjj asdf \\t dkfjke \\t jkdf"}, {" " "}
f[x_] := Sin[x^2]/(Cos[x]/E^x)

x = {"dddt ejkrjke dfjj asdf \\t dkfjke \\t jkdf"}, {" " "}
f[x_] := Sin[x^2]/(Cos[x]/E^x)

x = {"asdf 5 34 dkfjke jkdf"}, {" " "}

```

```
In[147]:=
(* !!f:\Mathe/Daten/AAA_f (* win3.1 etc. *) *)
```

14.2.3. Abspeichern von Output

■ Mémoriser l'output

Studiere: ■ Etudie:

```
In[148]:=
?>

x > y yields True if x is determined to be greater than y. x1 >
x2 > x3 yields True if the xi form a strictly decreasing sequence. Mehr...
```

```
In[149]:=
?>>

expr >> filename writes expr to a file. Put[expr1,
expr2, ... , "filename"] writes a sequence of expressions expr1 to a file. Mehr...
```

```
In[150]:=
?>>>

expr >>> filename appends expr to a file. PutAppend[expr1,
expr2, ... , "filename"] appends a sequence of expressions expr1 to a file. Mehr...
```

```
In[151]:=
?Put

expr >> filename writes expr to a file. Put[expr1,
expr2, ... , "filename"] writes a sequence of expressions expr1 to a file. Mehr...
```

Probiere aus: ■ Essaie:

```
In[152]:=
Table[f[n], {n, 20}] >>
C:\work\MathematicaData\AAneuDaten
```

```
In[153]:=
(* Table[f[n], {n, 20}] >>
f:\Mathe/Daten/neuDaten (* win3.1 etc. *) *)
```

```
In[154]:=
!! C:\work\MathematicaData\AAneuDaten

{E*Tan[1], E^2*Sec[2]*Sin[4], E^3*Sec[3]*Sin[9], E^4*Sec[4]*Sin[16],
E^5*Sec[5]*Sin[25], E^6*Sec[6]*Sin[36], E^7*Sec[7]*Sin[49],
E^8*Sec[8]*Sin[64], E^9*Sec[9]*Sin[81], E^10*Sec[10]*Sin[100],
E^11*Sec[11]*Sin[121], E^12*Sec[12]*Sin[144], E^13*Sec[13]*Sin[169],
E^14*Sec[14]*Sin[196], E^15*Sec[15]*Sin[225], E^16*Sec[16]*Sin[256],
E^17*Sec[17]*Sin[289], E^18*Sec[18]*Sin[324], E^19*Sec[19]*Sin[361],
E^20*Sec[20]*Sin[400]}
```

```
In[155]:=
(* !!f:\Mathe/Daten/neuDaten (* win3.1 etc. *) *)
```

```
In[156]:=
Put[Table[f[n], {n, 20}], Sin[x], "Hallo",
"C:\work\MathematicaData\AAneuDaten"]
```



```
In[157]:=
(* Put[Table[f[n], {n, 20}], Sin[x], "Hallo",
  "f:\Mathe/Daten/neuDaten" *) (* win3.1 etc. *)

In[158]:=
!! C:\\work\\MathematicaData\\AAneuDaten

{E*Tan[1], E^2*Sec[2]*Sin[4], E^3*Sec[3]*Sin[9], E^4*Sec[4]*Sin[16],
 E^5*Sec[5]*Sin[25], E^6*Sec[6]*Sin[36], E^7*Sec[7]*Sin[49],
 E^8*Sec[8]*Sin[64], E^9*Sec[9]*Sin[81], E^10*Sec[10]*Sin[100],
 E^11*Sec[11]*Sin[121], E^12*Sec[12]*Sin[144], E^13*Sec[13]*Sin[169],
 E^14*Sec[14]*Sin[196], E^15*Sec[15]*Sin[225], E^16*Sec[16]*Sin[256],
 E^17*Sec[17]*Sin[289], E^18*Sec[18]*Sin[324], E^19*Sec[19]*Sin[361],
 E^20*Sec[20]*Sin[400]}
{{Sin["asdf 5 34 dkfjke jkdf"]}, {Sin["  " ]}}
"Hallo"

In[159]:=
(* !!f:\Mathe/Daten/neuDaten *) (* win3.1 etc. *)
```

Was ist mit den Daten von 14.2.3 passiert?

Aue s'est-il passé avec les données de 14.2.3?

```
In[160]:=
2.^0.5

Out[160]=
1.41421

In[161]:=
2.^0.5 >> C:\\work\\MathematicaData\\AAneuDaten1

In[162]:=
(* 2.^0.5 >> f:\Mathe/Daten/neuDaten *)
(* win3.1 etc. *)

In[164]:=
!! C:\\work\\MathematicaData\\AAneuDaten1

1.4142135623730951

In[165]:=
(* !!f:\Mathe/Daten/neuDaten *) (* win3.1 etc. *)
```

Wieso ist das abgespeicherte Resultat genauer als das auf dem Schirm ausgegebene Resultat?

■ Pourquoi le résultat mémorisé est-il plus exact que le résultat sorti sur l'écran?

14.3. Manipulation von Strings

■ Manipulation de Strings

Studiere die folgenden Befehle:

■ Etudie les ordres suivants:

```
In[166]:=
?Read

Read[stream] reads one expression from an input stream, and returns the expression.
Read[stream, type] reads one object of the specified type. Read[stream, {type1,
type2, ... }] reads a sequence of objects of the specified types. Mehr...
```

In[167]:=

?ReadList

ReadList["file"] reads all the remaining expressions in a file, and returns a list of them. ReadList["file", type] reads objects of the specified type from a file, until the end of the file is reached. The list of objects read is returned. ReadList["file", {type1, type2, ...}] reads objects with a sequence of types, until the end of the file is reached. ReadList["file", types, n] reads only the first n objects of the specified types. **Mehr...**

In[168]:=

?OpenAppend

OpenAppend["file"] opens a file to append output to it, and returns an OutputStream object. **Mehr...**

In[169]:=

?OpenRead

OpenRead["file"] opens a file to read data from, and returns an InputStream object. **Mehr...**

In[170]:=

?StringDrop

StringDrop["string", n] gives "string" with its first n characters dropped. StringDrop["string", -n] gives "string" with its last n characters dropped. StringDrop["string", {n}] gives "string" with its nth character dropped. StringDrop["string", {m, n}] gives "string" with characters m through n dropped. StringDrop[{s1, s2, ...}, spec] gives the list of results for each of the si. **Mehr...**

In[171]:=

?StringInsert

StringInsert["string", "snew", n] yields a string with "snew" inserted starting at position n in "string". StringInsert["string", "snew", -n] inserts at position n from the end of "string". StringInsert["string", "snew", {n1, n2, ...}] inserts a copy of "snew" at each of the positions ni. StringInsert[{s1, s2, ...}, "snew", n] gives the list of results for each of the si. **Mehr...**

In[172]:=

?StringJoin

"s1" <> "s2" <> ... , StringJoin["s1", "s2", ...] or StringJoin[{s1, "s2", ...}] yields a string consisting of a concatenation of the si. **Mehr...**

In[173]:=

?StringReplace

StringReplace["string", s -> sp] or StringReplace["string", {s1 -> sp1, s2 -> sp2, ...}] replaces the string expressions si by spi whenever they appear as substrings of "string". StringReplace["string", srules, n] does only the first n replacements. StringReplace[{s1, s2, ...}, srules] gives the list of results for each of the si. **Mehr...**

In[174]:=

?StringReverse

StringReverse["string"] reverses the order of the characters in "string". **Mehr...**

In[175]:=

?StringTake

StringTake["string", n] gives a string containing the first n characters in "string". StringTake["string", -n] gives the last n characters in "string". StringTake["string", {n}] gives the nth character in "string". StringTake["string", {m, n}] gives characters m through n in "string". StringTake[{s1, s2, ... }, spec] gives the list of results for each of the si. **Mehr...**

In[176]:=

?StringLength

StringLength["string"] gives the number of characters in a string. **Mehr...**

In[177]:=

?StringPosition

StringPosition["string", "sub"] gives a list of the starting and ending character positions at which "sub" appears as a substring of "string". StringPosition["string", patt] gives all positions at which substrings matching the general string expression patt appear in "string". StringPosition["string", patt, n] includes only the first n occurrences of patt. StringPosition["string", {patt1, patt2, ... }] gives positions of all the patti. StringPosition[{s1, s2, ... }, p] gives the list of results for each of the si. **Mehr...**

In[178]:=

?StringMatchQ

StringMatchQ["string", patt] tests whether string matches the string pattern patt. StringMatchQ["string", RegularExpression["regex"]] tests whether string matches the specified regular expression. StringMatchQ[{s1, s2, ... }, p] gives the list of results for each of the si. **Mehr...**

In[179]:=

?StringQ

StringQ[expr] gives True if expr is a string, and False otherwise.

In[180]:=

?StringToStream

StringToStream["string"] opens an input stream for reading from a string. **Mehr...**

In[181]:=

?WriteString

WriteString[channel, expr1, expr2, ...] converts the expri to strings, and then writes them in sequence to the specified output channel. **Mehr...**

In[182]:=

?ToString

ToString[expr] gives a string corresponding to the printed form of expr in OutputForm. ToString[expr, form] gives the string corresponding to output in the specified form. **Mehr...**

Probiere aus: ■ **Essaie:**

In[183]:=

```
Table[StringJoin["daten.", ToString[i]],{i,6}]
```

Out[183]=

```
{daten.1, daten.2, daten.3, daten.4, daten.5, daten.6}
```

14.4. Eingabe- und Ausgabeform

■ Formes d'entrée et de sortie

Studiere die folgenden Befehle:

■ Etudie les ordres suivants:

In[184]:=

?InputForm

InputForm[expr] prints as a version of expr suitable for input to Mathematica. Mehr...

In[185]:=

?OutputForm

OutputForm[expr] prints as a two-dimensional representation of expr using only keyboard characters. Mehr...

Beispiele: ■ Exemples:

In[186]:=

```
Clear[a,x,y];
a = x^5/x^2 y +x^y^5
```

Out[187]=

$$x^y^5 + x^3 y$$

In[188]:=

InputForm[a]

Out[188]//InputForm=

$$x^y^5 + x^3*y$$

In[189]:=

OutputForm[a]

Out[189]//OutputForm=

$$x^y^5 + x^3 y$$

In[190]:=

```
a >> C:\\work\\MathematicaData\\AAneuDaten2
```

In[191]:=

```
(* a >> f:\Mathe/Daten/neuDaten *) (* win3.1 etc. *)
```

In[192]:=

```
!! C:\\work\\MathematicaData\\AAneuDaten2
```

$$x^y^5 + x^3*y$$

In[193]:=

```
(* !!f:\Mathe/Daten/neuDaten *) (* win3.1 etc. *)
```

In[194]:=

```
Read["C:\\work\\MathematicaData\\AAneuDaten2"]
```

Out[194]=

$$x^y^5 + x^3 y$$

```

In[195]:=
  (* Read["f:\Mathe/Daten/neuDaten"](* win3.1 etc. *) *)

In[196]:=
  b = Read["C:\\work\\MathematicaData\\AAneuDaten2"]

Out[196]=
  EndOfFile

In[197]:=
  (* b = Read["f:\Mathe/Daten/neuDaten"] *)
  (* win3.1 etc. *)

In[199]:=
  b

Out[199]=
  EndOfFile

In[200]:=
  !! C:\\work\\MathematicaData\\AAneuDaten2

  x^y^5 + x^3*y

In[201]:=
  (* !!f:\Mathe/Daten/neuDaten *) (* win3.1 etc. *)

In[202]:=
  Close["C:\\work\\MathematicaData\\AAneuDaten2"]

Out[202]=
  C:\work\MathematicaData\AAneuDaten2

In[203]:=
  (* Close["f:\Mathe/Daten/neuDaten"] *)
  (* win3.1 etc. *)

In[205]:=
  b = Read["C:\\work\\MathematicaData\\AAneuDaten2"]

Out[205]=
  xy + x3 y

In[206]:=
  (* b = Read["f:\Mathe/Daten/neuDaten"] *)
  (* win3.1 etc. *)

In[208]:=
  Close["C:\\work\\MathematicaData\\AAneuDaten2"]

Out[208]=
  C:\work\MathematicaData\AAneuDaten2

In[209]:=
  (* Close["f:\Mathe/Daten/neuDaten"] *)
  (* win3.1 etc. *)

```

14.5. Uebersetzen von Ausdrücken in andere Programmiersprachen und Manipulation von Sourcecode

■ Traduire des expressions en d'autres langages de programmation et manipulation de sourcecode

Uebersetzungen

■ Traduction

Studiere die folgenden Befehle:

■ Etudie les ordres suivants:

In[211]:=

?CForm

CForm[expr] prints as a C language version of expr. Mehr...

In[212]:=

?FortranForm

FortranForm[expr] prints as a Fortran language version of expr. Mehr...

In[213]:=

?TeXForm

TeXForm[expr] prints as a TeX version of expr. Mehr...

In[214]:=

?Splice

Splice["file"] splices Mathematica output into an external file. It takes text enclosed between < * and * > in the file, evaluates the text as Mathematica input, and replaces the text with the resulting Mathematica output. Mehr...

Beispiele: ■ Exemple:

In[215]:=

```
Clear[a];
a = x^5/z^2 y + x^y^5 +
      ( x^2 Sin[x^5/z^2 y + x^y^5]);
```

In[217]:=

CForm[a]

Out[217]//CForm=

```
Power(x,Power(y,5)) + (Power(x,5)*y)/Power(z,2) +
Power(x,2)*Sin(Power(x,Power(y,5)) +
(Power(x,5)*y)/Power(z,2))
```

In[218]:=

FortranForm[a]

Out[218]//FortranForm=

```
x**y**5 + (x**5*y)/z**2 +
- x**2*Sin(x**y**5 + (x**5*y)/z**2)
```

In[219]:=

TeXForm[a]

Out[219]//TeXForm=

```
x^{y^5}+\frac{y x^5}{z^2}+\sin
\left(x^{y^5}+\frac{y x^5}{z^2}\right) x^2
```

Manipulation von Sourcecode

■ Manipulation de sourcecode

Im folgenden Beispiel wird gezeigt, wie in den Source-Code eines externen Programms (z.B. in C) direkt *Mathematica*-Ausdrücke eingesetzt und dann von *Mathematica* übersetzt werden können. Der externe Programmteil befindet sich im File AAA.mc. Das übersetzte Programm wird in AAA.c gespeichert!!!!!!

■ Dans l'exemple suivant on montre comme on peut mettre des expressions de *Mathematica* directement dans le Source-Code d'un autre programme extérieur (p.ex. dans C), ensuite ses expressions peuvent être traduites par *Mathematica*. La partie extérieur du programme se trouve dans le fichier AAA.mx resp. AAA.mc. Le programme traduit est mémorisé dans AAA.x resp. AAA.c !!!!!!!

```
In[220]:=
  Sin[3] + Cos[3] >> C:\work\MathematicaData\AAA.mx

In[221]:=
  !! C:\work\MathematicaData\AAA.mx

  Cos[3] + Sin[3]

In[222]:=
  (* !!f:\Mathe\Daten\AAA.mc *) (* win3.1 etc. *)

In[223]:=
  ?Splice

  Splice["file"] splices Mathematica output into an external file. It takes text
  enclosed between < * and * > in the file, evaluates the text as Mathematica
  input, and replaces the text with the resulting Mathematica output. Mehr...

In[224]:=
  Splice["C:\work\MathematicaData\AAA.mx"]

Out[224]=
  C:\work\MathematicaData\AAA.mx

In[225]:=
  (* Splice["f:\Mathe\Daten\AAA.mc"] *)
  (* win3.1 etc. *)

In[227]:=
  !! C:\work\MathematicaData\AAA.mx

  Cos[3] + Sin[3]

In[228]:=
  (* !!f:\Mathe\Daten\AAA.c *) (* win3.1 etc. *)
```

14.6. Formate

■ Formats

Allgemeines

■ Généralités

Studiere die folgenden Befehle:

■ Etudie les ordres suivants:

```
In[229]:=
```

```
?Subscripted
```

```
System`Subscripted
```

```
In[230]:=
```

```
?Superscript
```

```
Superscript[x, y] is an object that formats as x with a superscript y. Mehr...
```

```
In[231]:=
```

```
?SequenceForm
```

```
SequenceForm[expr1, expr2, ... ] prints as the  
textual concatenation of the printed forms of the expr1. Mehr...
```

Probiere aus: ■ Etudie:

```
In[232]:=
```

```
Subscripted[abc[145]]
```

```
Out[232]=
```

```
abc145
```

```
In[233]:=
```

```
SequenceForm[uvw, Superscript[251]]
```

```
Out[233]=
```

```
uvw251
```

Ein Anwendungsbeispiel

■ Un exemple d'application

```
In[234]:=
```

```
Remove[a, n, m];  
Format[a[n_, m_]] := Subscripted[a[n, m]];  
Array[a, {2, 2}] // MatrixForm
```

```
Out[236]//MatrixForm=
```

$$\begin{pmatrix} a_{1,1} & a_{1,2} \\ a_{2,1} & a_{2,2} \end{pmatrix}$$

"Putzmaschine" einsetzen

■ Employer la "machine de nettoyage"

```
In[237]:=
  (* Old Form: Remove["Global`*"] *)
```

```
In[238]:=
  Remove["Global`*"]
```