

Übungen in Analysis \diamond Exercices en analyse \diamond Type I1 \diamond I / 8

Probl. 1 $f(x) = e^{(x^2 - \cos(2x))} \rightsquigarrow f$ gerade/ ungerade? • f paire/ impaire?

Probl. 2 $f(x) = y = e^{-x^2}$

(a) $x \geq 0 \rightsquigarrow f^{-1}(x) = ?$ Skizze! • *Esquisse!*

(b) $f^{-1}(0.5) \approx ?$

Probl. 3 $\log(x^2) + \log\left(\frac{1}{x}\right) - \log(x) = ?$

Probl. 4 $\sin\left(x + \frac{\pi}{3}\right) = \sin(x) \cdot (?) + \cos(x) \cdot (?)$

(a) $\sin\left(x + \frac{\pi}{3}\right) = \sin(x) \cdot (?) + \cos(x) \cdot (?)$

(b) $\tan\left(x + \frac{\pi}{3}\right) = \dots ? \dots$

Probl. 5 $r(\varphi) = 1 + \cos\left(\frac{\varphi}{2}\right) \rightsquigarrow$ Polar... Skizze! • *Polaire... esquisse!*

Probl. 6 $2 \cdot 3^x = 5^x \rightsquigarrow x = ?$

Probl. 7 $0.367367\dots = \frac{p}{q}$, $p, q \in \mathbb{N} \rightsquigarrow p, q = ?$

Probl. 8 $\langle a_n \rangle = \left\langle \frac{\sin\left(3\pi + \frac{4}{5}n^2\right)}{n^2} \right\rangle \rightsquigarrow a_n \rightarrow ?$

Probl. 9 $\langle a_n \rangle = \left\langle \frac{n^2 - 2n + 5}{n^3 + n^2 + 1} \right\rangle \rightsquigarrow a_n \rightarrow ?$

Probl. 10 $\langle a_n \rangle = \left\langle \frac{\ln(n)}{n^2} \right\rangle \rightsquigarrow a_n \rightarrow ?$

Hinweis: Skizze! • *Indication: Exquisse!* $\rightsquigarrow \ln(n), n$

Probl. 11 $\langle a_n \rangle = \left\langle \left(1 + \frac{1}{n} + \frac{1}{n^2}\right) \cdot \left(5 + \frac{2+n}{n}\right) \right\rangle \rightsquigarrow a_n \rightarrow ?$

Probl. 12 $\langle a_n \rangle = \left\langle e^{\sin\left(\pi + \frac{1}{n}\right)} \right\rangle \rightsquigarrow a_n \rightarrow ?$